

The Three-Nucleon Force - Revisited

Some Historical Thoughts

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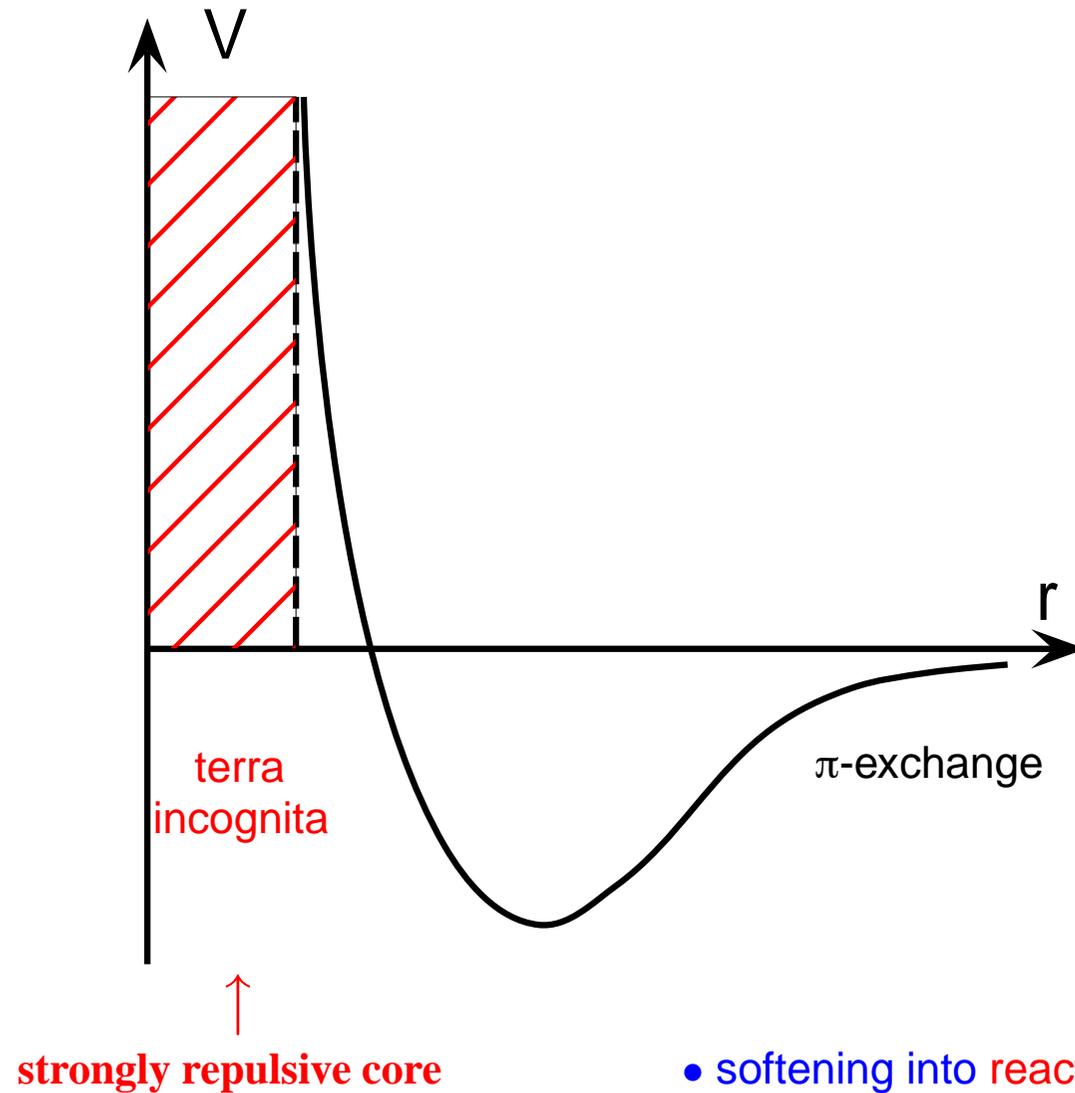
MIT 1970/71

Nuclear Structure in Terms of
Realistic Two-Nucleon Potential

Outline

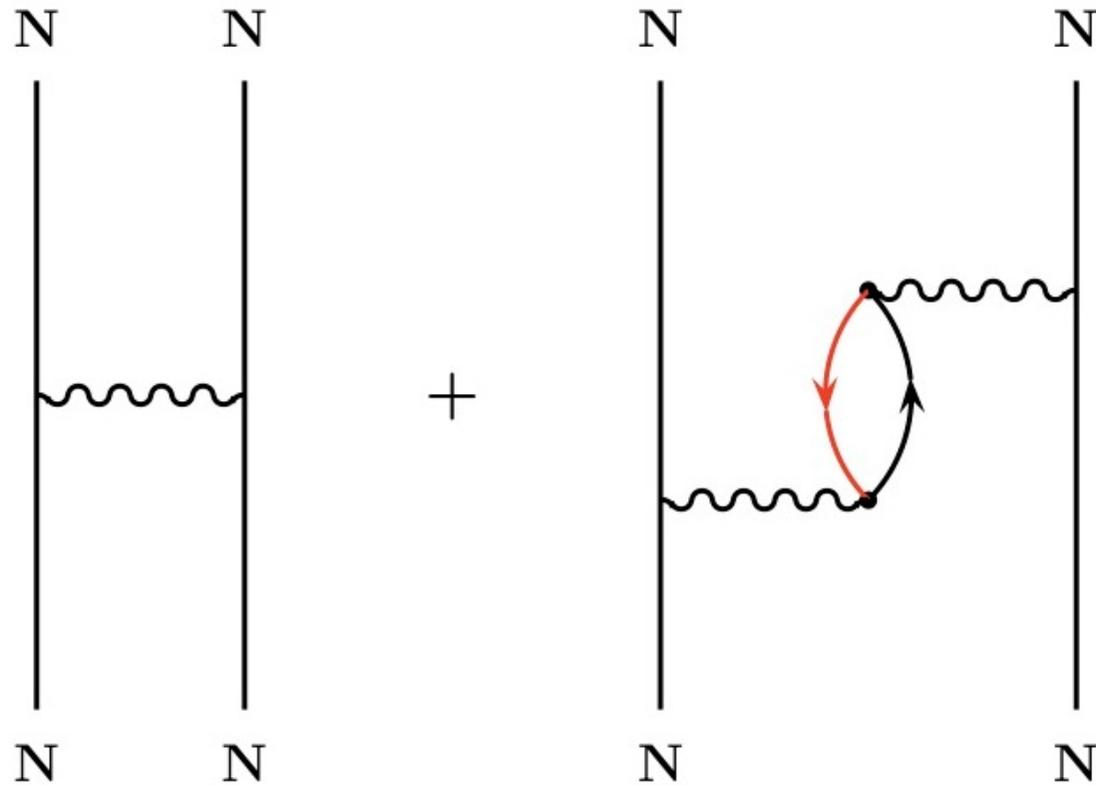
- Shell Model of Nuclear Structure - Distant Past
- Few-Nucleon Systems - Test of Nuclear Dynamics
 - Choice of Hilbert Space and Hamiltonian
 - Technical Challenges
 - Celebrated Successes
 - Remaining Puzzles
- What Have We Learnt from all those Calculations?

Two-Nucleon Potential a Terrifying Beast



- softening into reaction matrix required
- super-soft core forbidden by MIT experimental theorem

Shell Model in Early Days



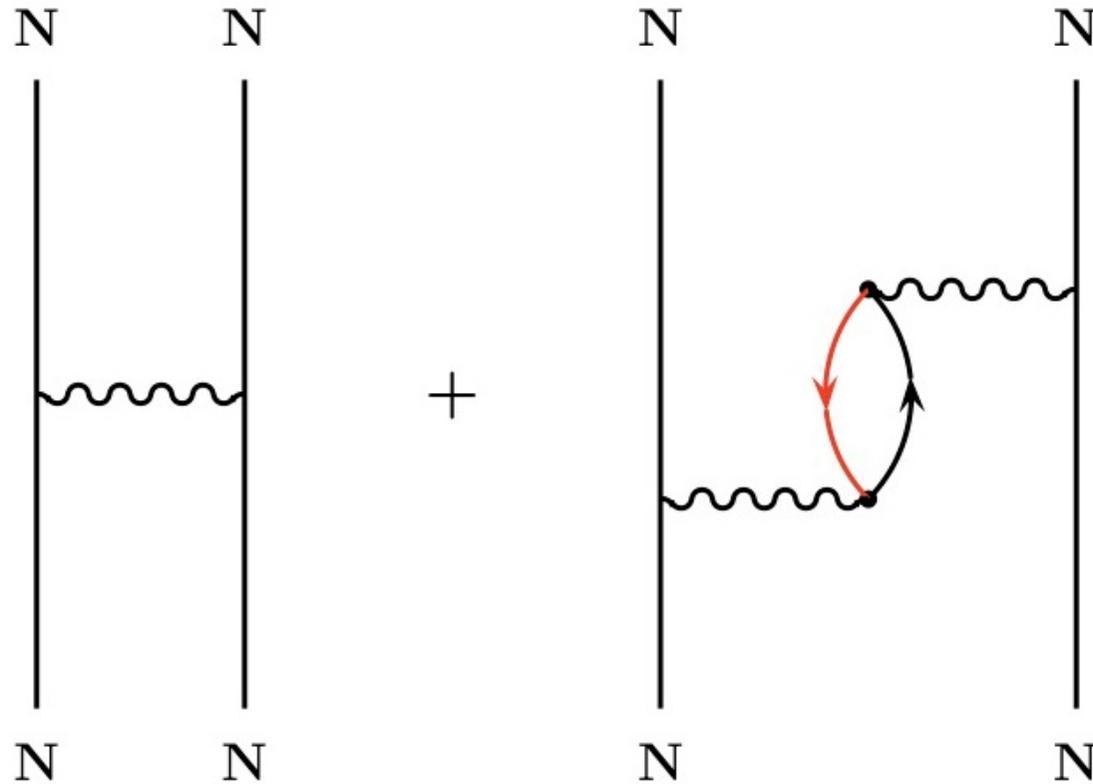
O^{18}
model space of
2N's in s-d shell

Effective Potential with *Core-Polarization*

Kuo, Brown and Bertsch:

"Theory correct, since agreement with data good!"

Shell Model in Early Days



O^{18}
model space of
2N's in s-d shell

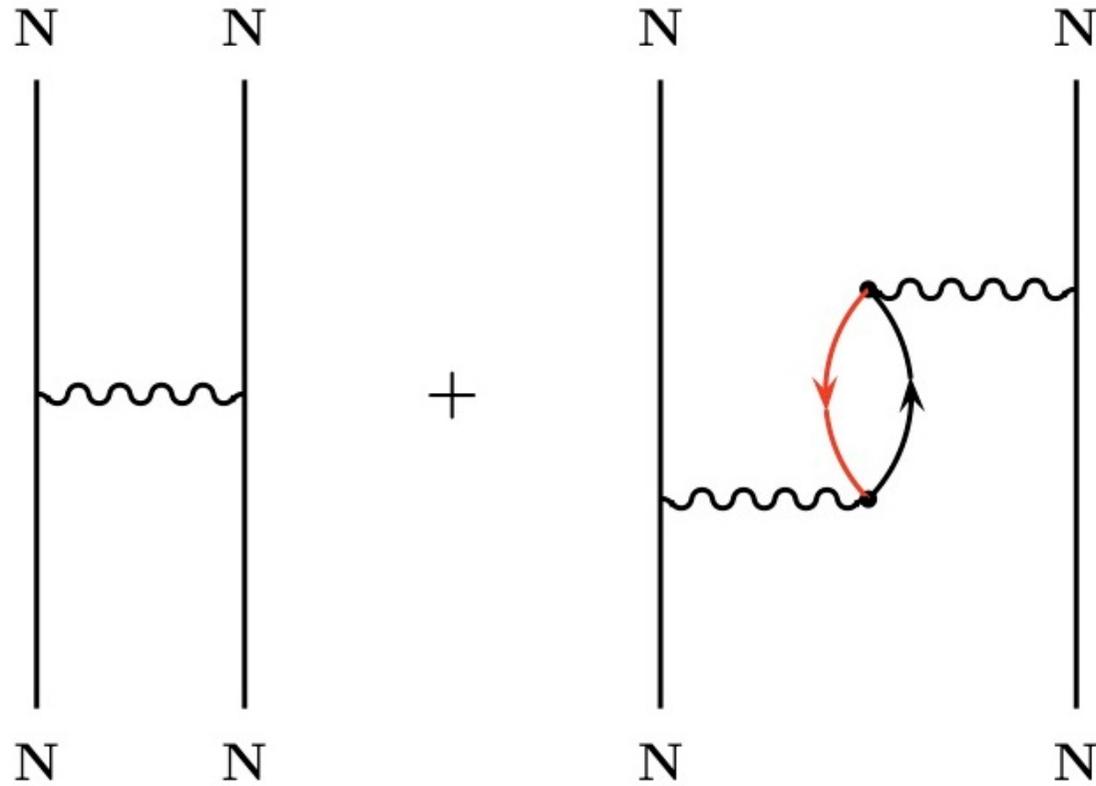
Effective Potential with *Core-Polarization*

Vary, Sauer, Wong:

"Calculation of core-polarization not converged"

Very sorry, wrong!

Shell Model in Early Days



O^{18}
model space of
2N's in s-d shell

Effective Potential with *Core-Polarization*

Barrett, Kirson - Schucan, Weidenmüller:

"Effective interaction not converging"

Shell Model Now - View of a Bystander

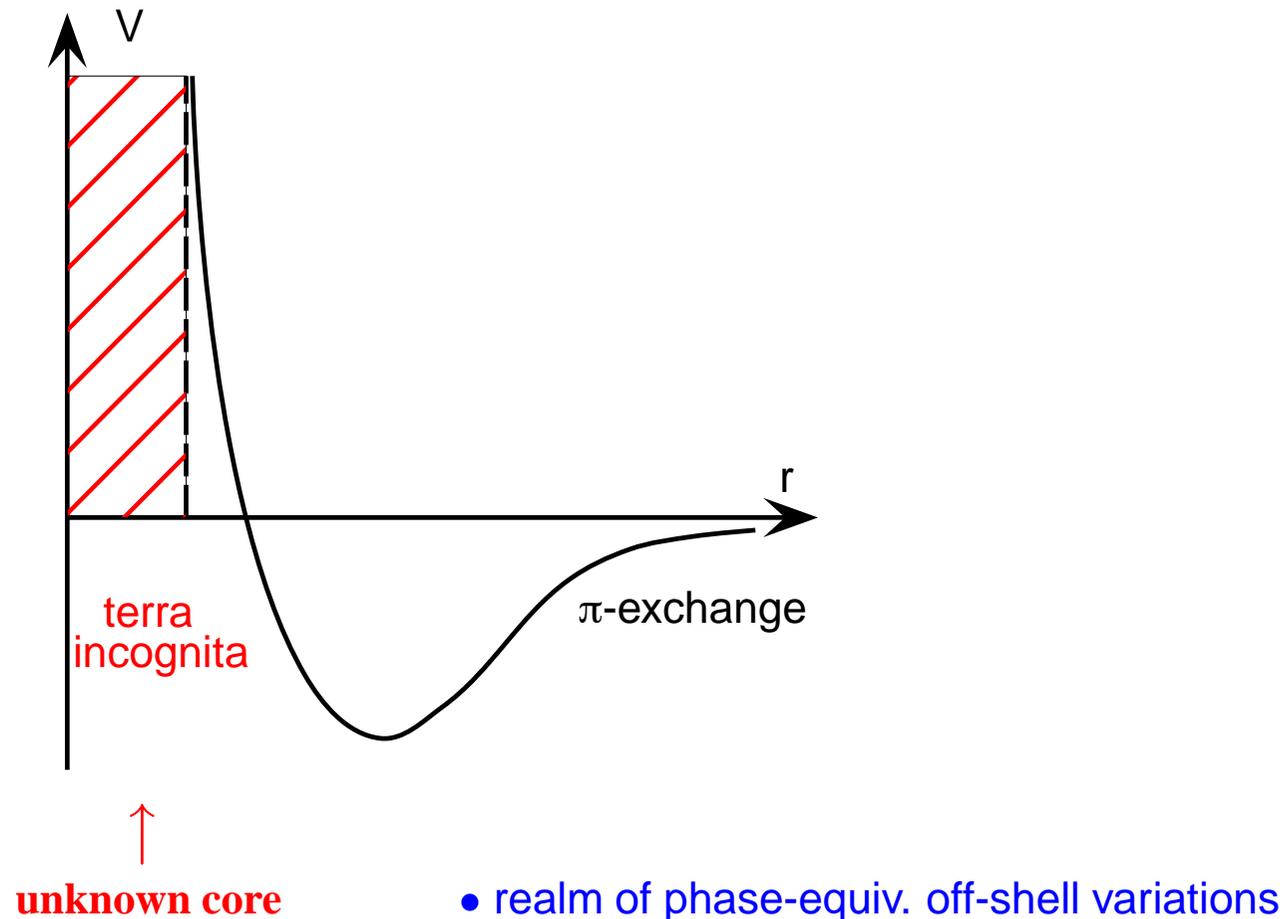
Core-Polarization Moved

from Effective Interaction to Model Space

Strategy

- Efficient Balance between Model Space and Effective Interaction
- Hilbert Space Truncated:
 - Many-Body Contributions to Effective Interaction
 - Effective Three-Nucleon Interaction**

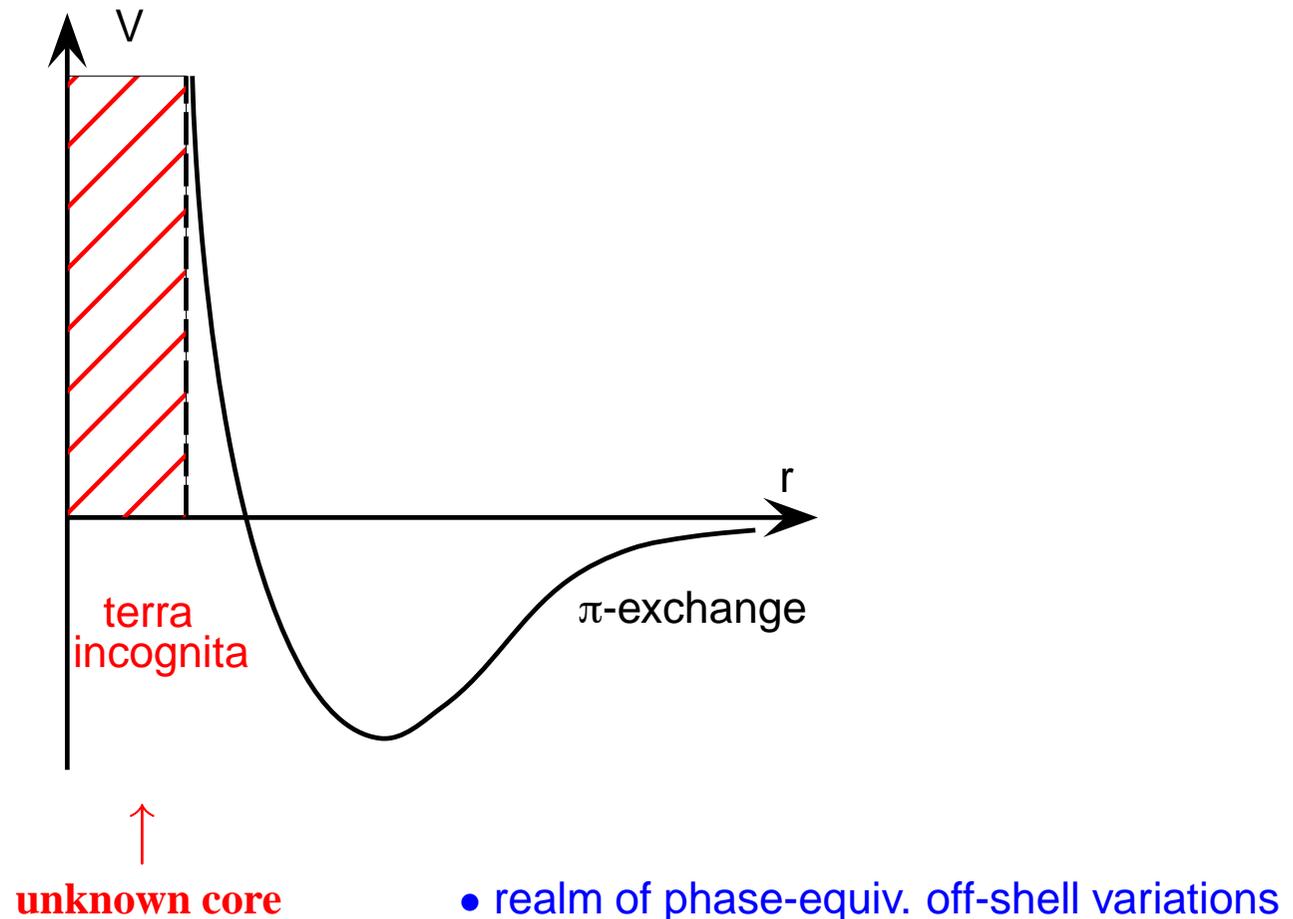
Two-Nucleon Potential a Terrible Beast



Hope: Off-shell information on 2N force from nuclear-structure results like O^{18}

Pradhan, PUS, Vary - no strategic exploration

Two-Nucleon Potential a Terrible Beast



Hope: Off-shell information on 2N force from nuclear-structure results like O^{18}

At that time an illusion - now *ab exitu* approach

Basic Assumption for Nuclear Structure and Reactions:

Rigid Nucleons Interact through 2N, 3N and ... Forces

Problems twofold and distinct:

- How to solve the many-nucleon problem for chosen forces? → **shell model**
- How to learn about nucleonic forces? How important is the genuine three-nucleon force? → **few-body physics**

Three- and Four-Nucleon Systems

Exactly Numerically Solvable - in Principle

Faddeev - Alt, Grassberger, Sandhas

3N and 4N Systems Theoretical Laboratories of Choice
for Studying Properties of Interaction between Nucleons.

Three- and Four-Nucleon Systems

bound states: ${}^3\text{H}, {}^3\text{He}, {}^4\text{He}$

3N reactions: $\text{N} + \text{d}$

4N reactions: $\text{N} + {}^3\text{H}$
 $\text{N} + {}^3\text{He}$
 $\text{d} + \text{d}$

multitude of hadronic reactions, coupled and with break-up,
with polarization, and corresponding em reactions

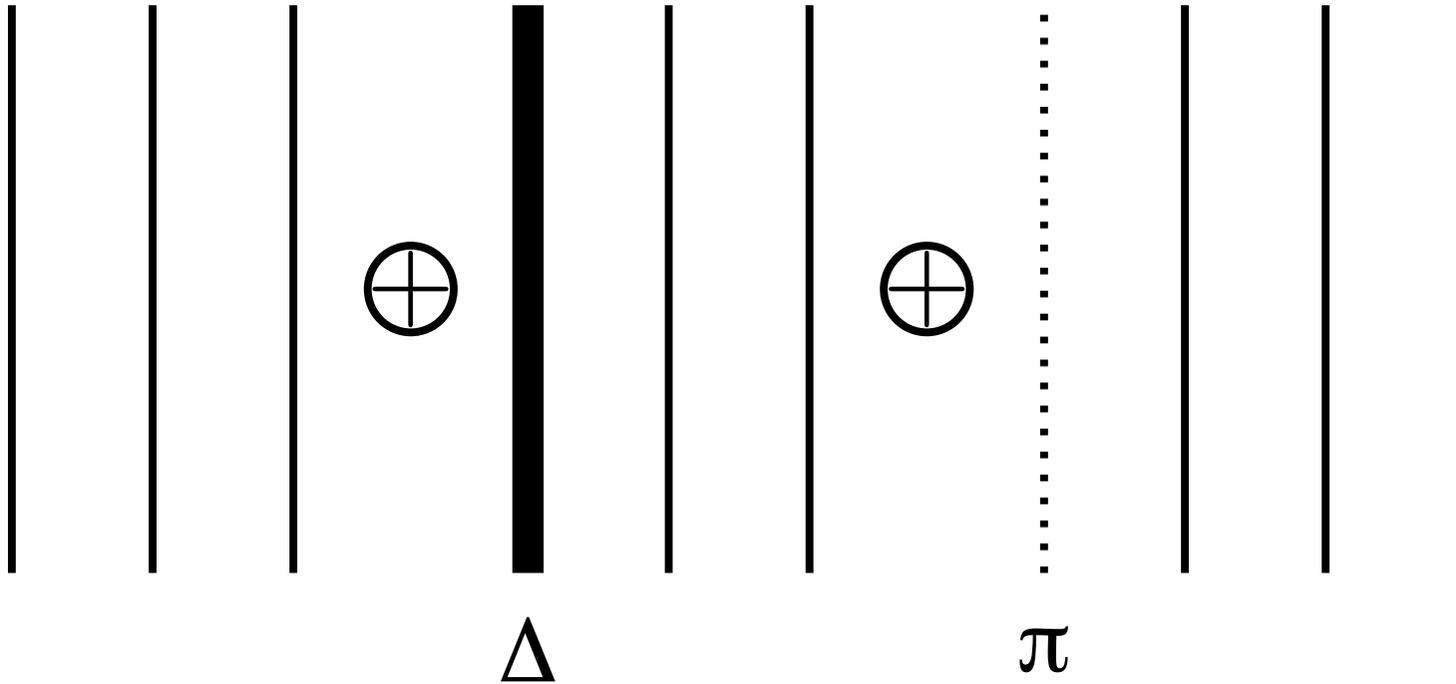
shown results obtained with A. Deltuva and A. C. Fonseca, Lisboa
our approach momentum space - not all theory groups can do all needed
calculations

our historic choice of $2N$ and $3N$ forces
more ambitious than low energy

- what are the important degrees of freedom up to 0.5 GeV c.m. energy?
- how can consistency between the forces be achieved?

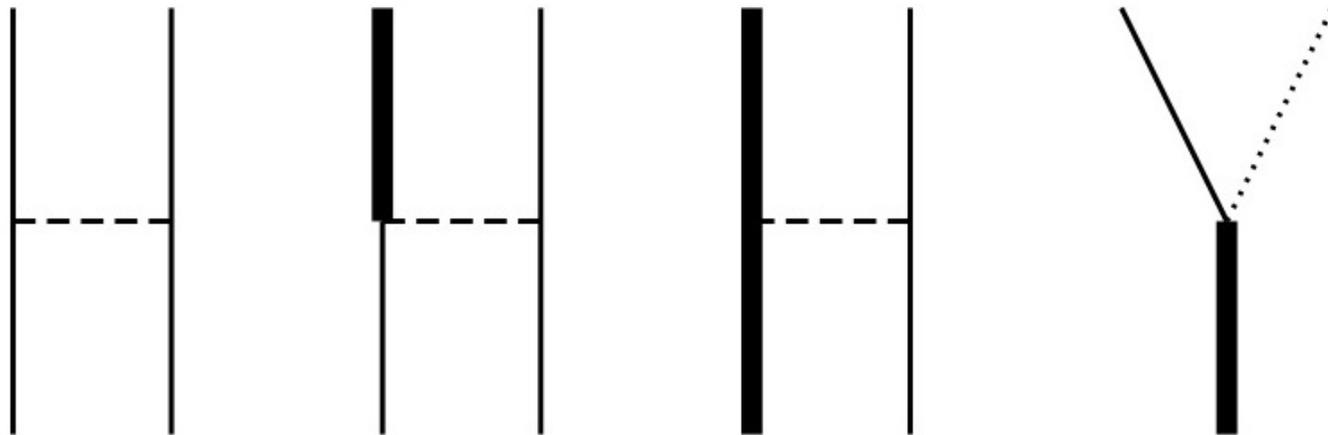
framework: old-fashioned meson theory

Hilbert space



dynamics up to 0.5 GeV c.m. energy:
single Δ excitation
single π channels

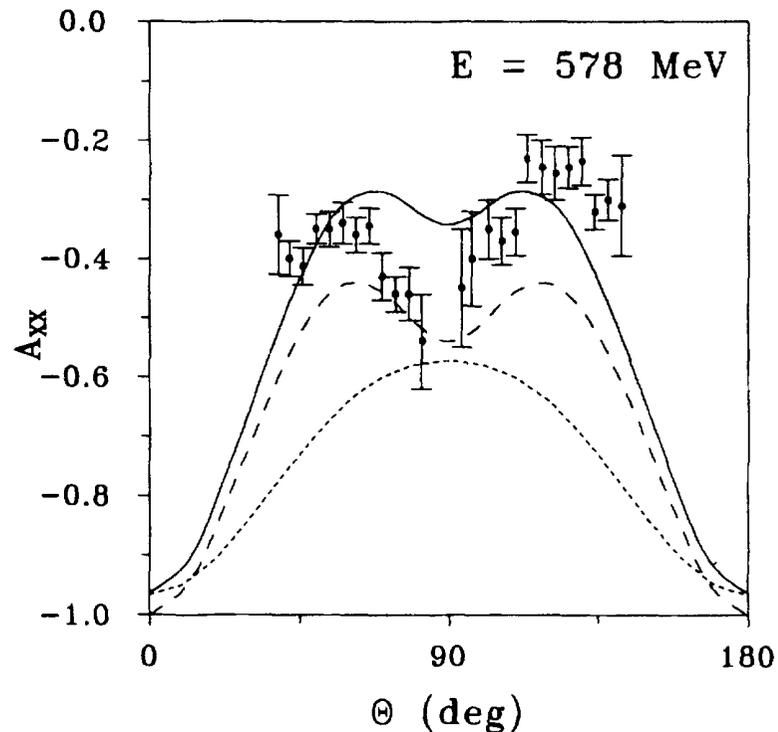
hamiltonian unifying nuclear phenomena at low and intermediate energies



novel scattering theory with particle production and absorption

- description of π N scattering
- unified description of NN and π NN dynamics
- nuclear structure with many-nucleon forces
- π -nucleus scattering with Δ -hole approach

unified description of NN and π NN dynamics



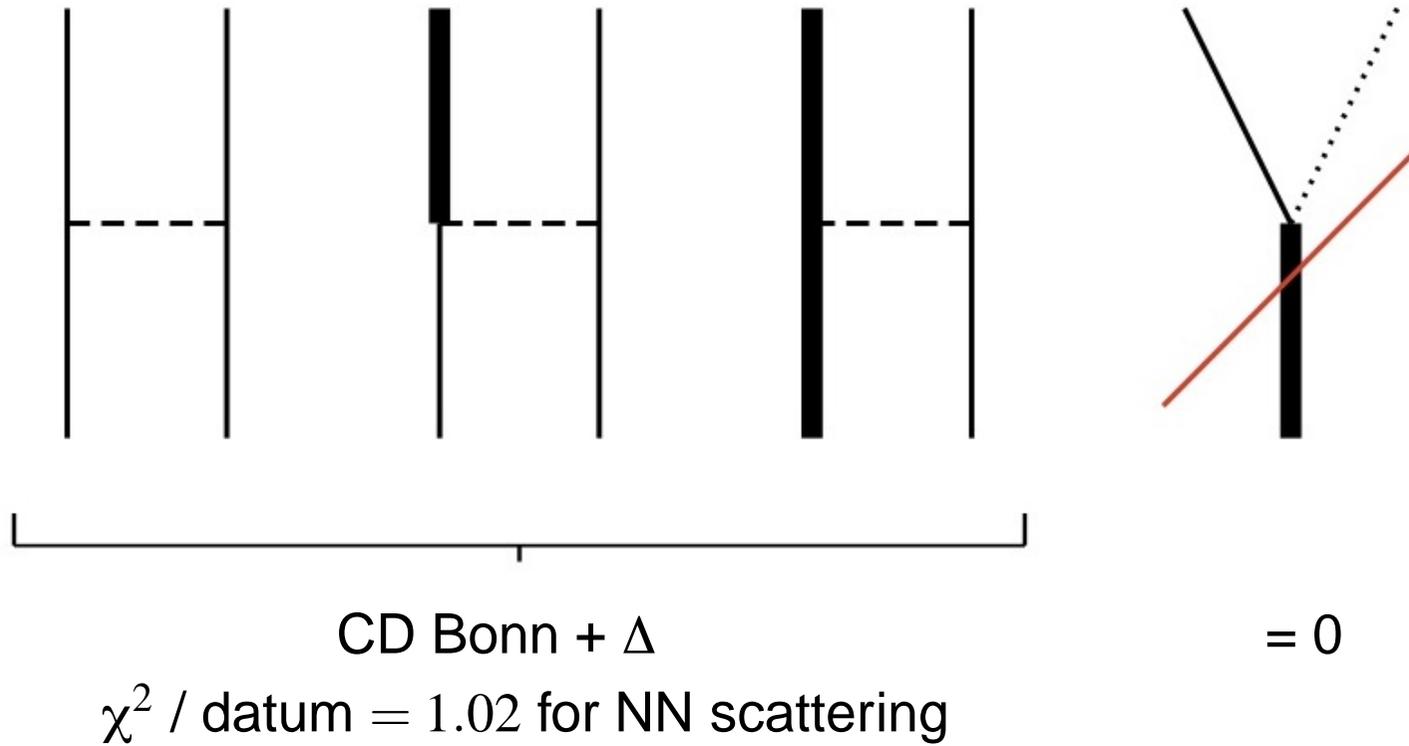
NN - π d scattering
Valcarce *et al* PRC 1994

test of $N\Delta$ potential

— quarks
- - - mesons
..... $N\Delta = 0$

dream of unifying low and intermediate energies ended with the end of pion factories - concentration on low-energy few-nucleon systems

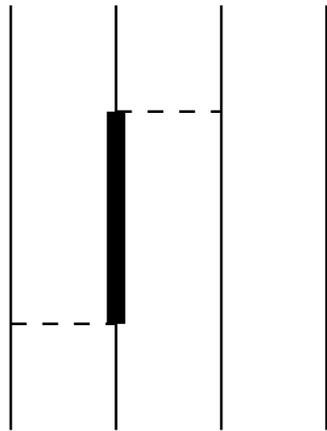
Hamiltonian for Low Energies



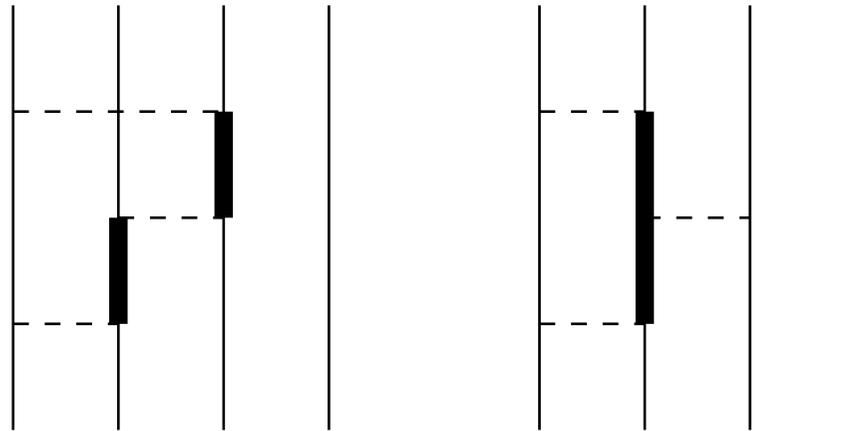
dynamic assumption: no **pionic channel**, Δ without width
no **irreducible many-baryon forces**

effective and consistent 2N, 3N and 4N forces

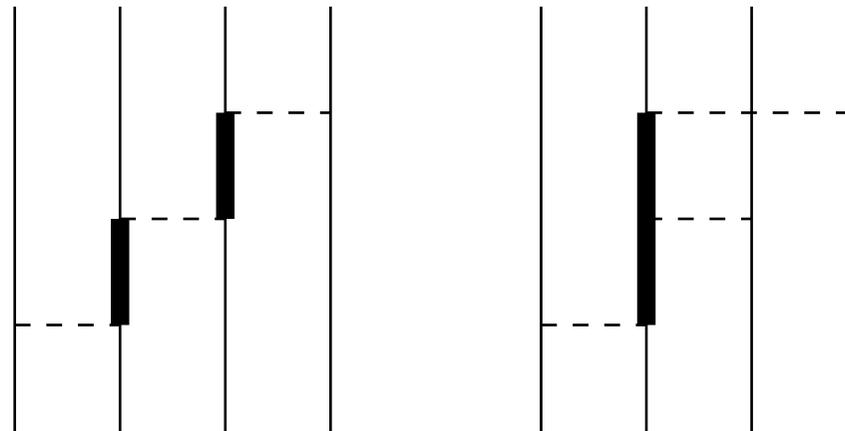
Fujita-Miyazawa



higher order 3N force



4N force



interesting relation to shell model

- coupled-channel approach with Δ -isobar

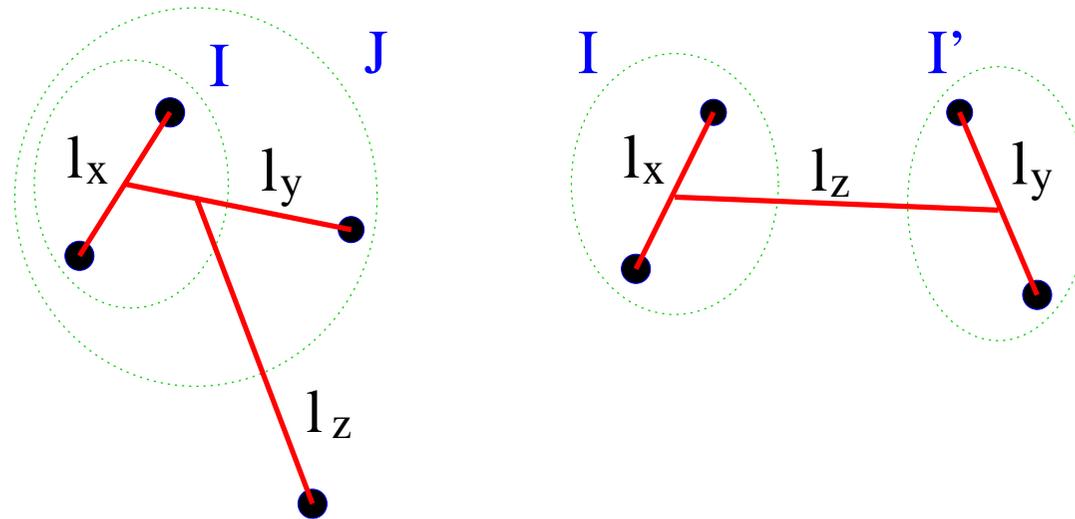
extension of nuclear Hilbert space yields effective many-nucleon interactions standing for genuine many-nucleon forces

- *ab initio* shell model

truncation of nuclear Hilbert space yields effective many-nucleon interactions even without genuine many-nucleon forces

Technical Challenges
in Few-Body Calculations
Enormous

example 4N scattering



- momentum-space partial-wave basis
- set of coupled integral equations in 3 variables
- kernel full of singularities, though integrable

numerical methods

- Gaussian integration
- spline interpolation
- up to 20000 partial waves,
20 Gaussian points for each momentum
⇒ system of $> 10^8$ linear equations,
size of the kernel $> 10^8$ GB
- summing up double Neumann series by Padé method
[*Phys. Rev. C* 75, 014005 (2007)]

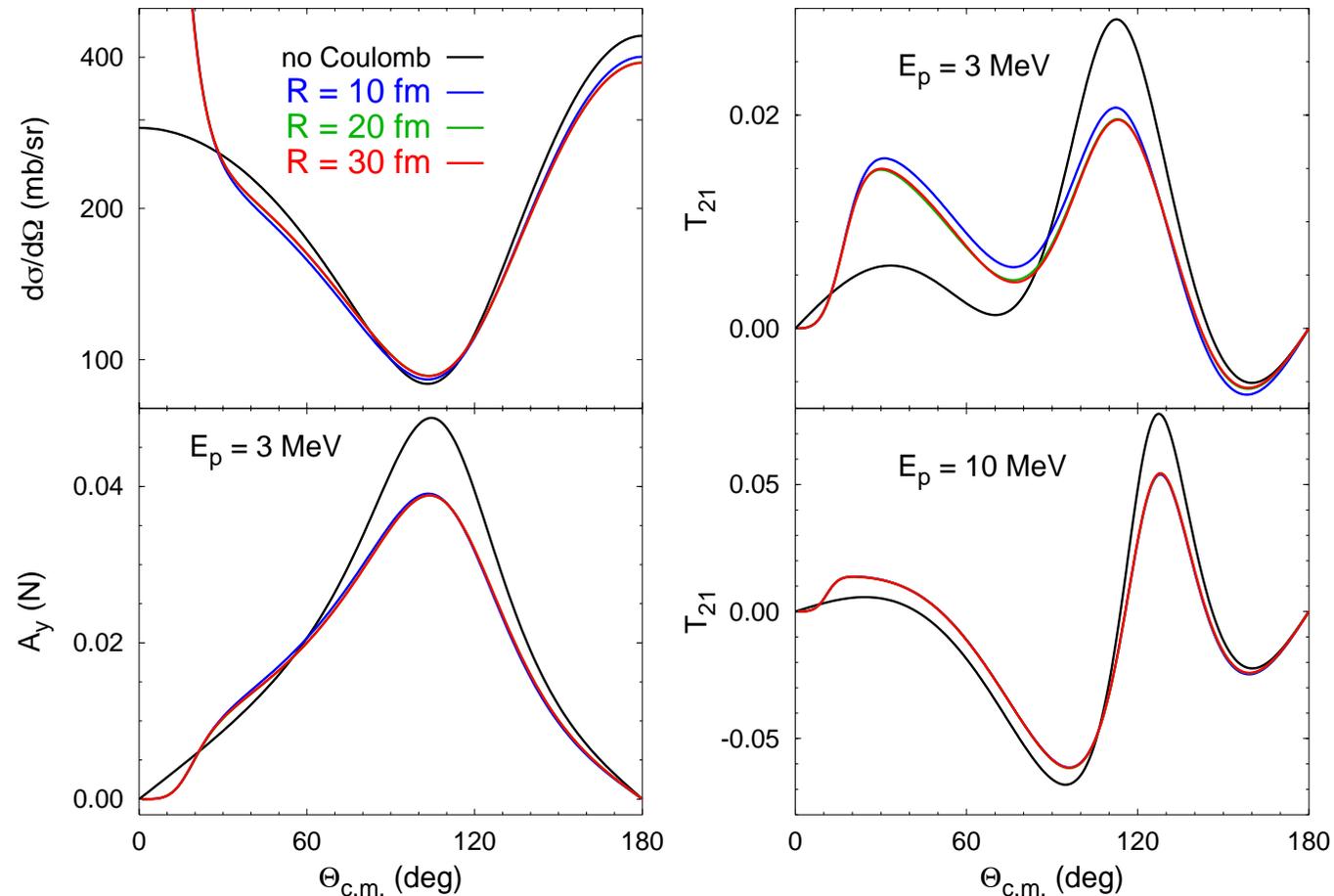
An Example for Nuclear Theory in the Supercomputing Era?

Coulomb Problem in Scattering

- experimentalists love reactions with charged particles - rich amount of accurate data
- Coulomb interaction hides nuclear dynamics and symmetries, e.g., charge asymmetry
- Coulomb interaction is nightmare for theorists

screening and renormalization works beautifully

example pd elastic: convergence with screening radius



our technical limitation: numerically too awkward in keV-neighbourhood of thresholds

Results for 3N and 4N Systems

3N and 4N bound states: binding

	${}^3\text{H}$	${}^3\text{He}$	${}^4\text{He}$
CD Bonn	8.00	7.26	26.18
CD Bonn + Δ	8.28	7.54	27.10
exp	8.48	7.72	28.30
ΔE_2	-0.51	-0.48	-2.80
$\Delta E_3(\text{FM})$	0.50	0.48	2.25
$\Delta E_3(\text{h.o.})$	0.29	0.28	1.30
ΔE_4			0.17

excited ${}^4\text{He}$ states seen as resonances in 4N scattering

3N and 4N bound states: binding

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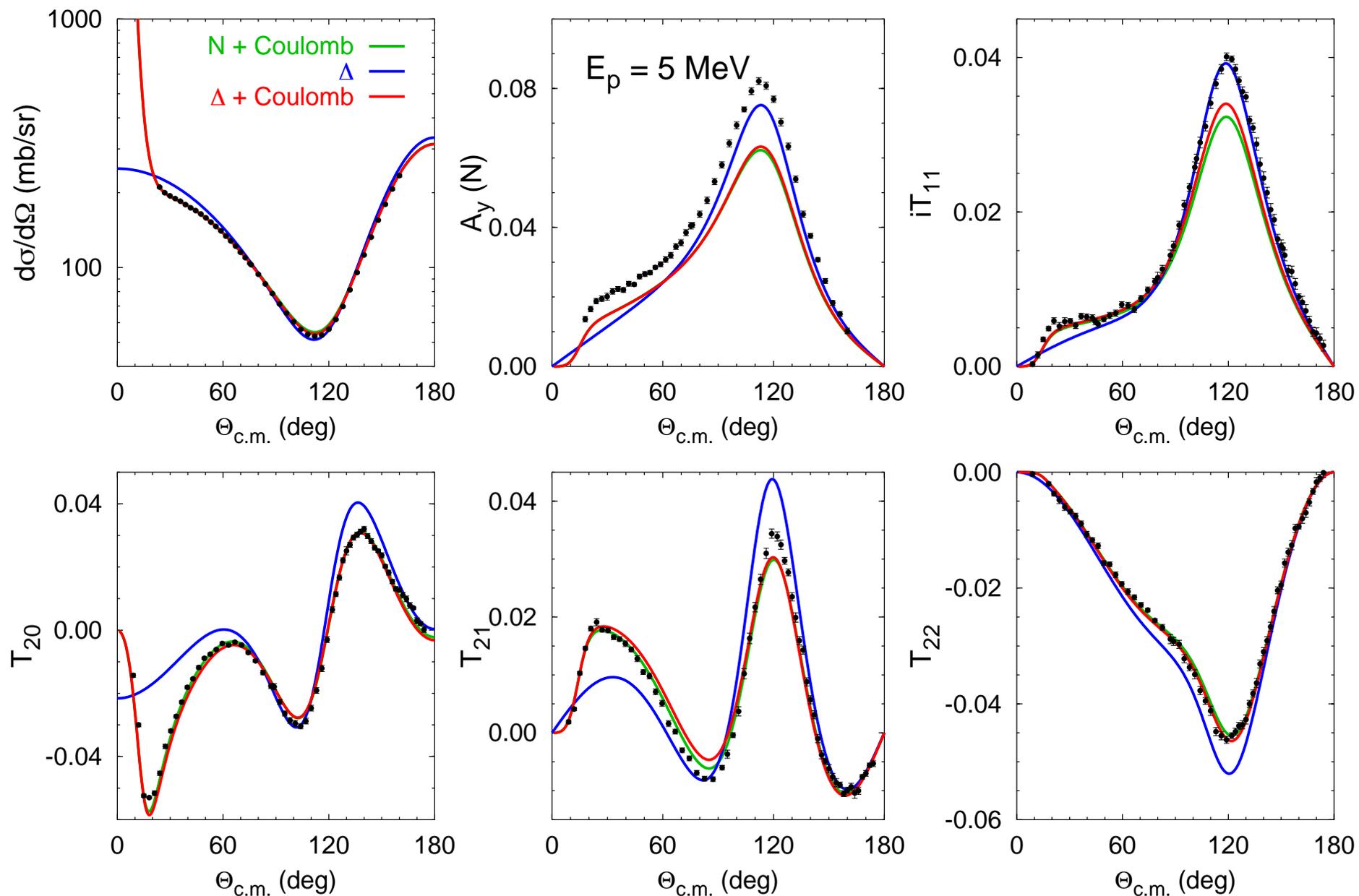
4N-force effect much smaller than 3N-force effect

3N and 4N reactions

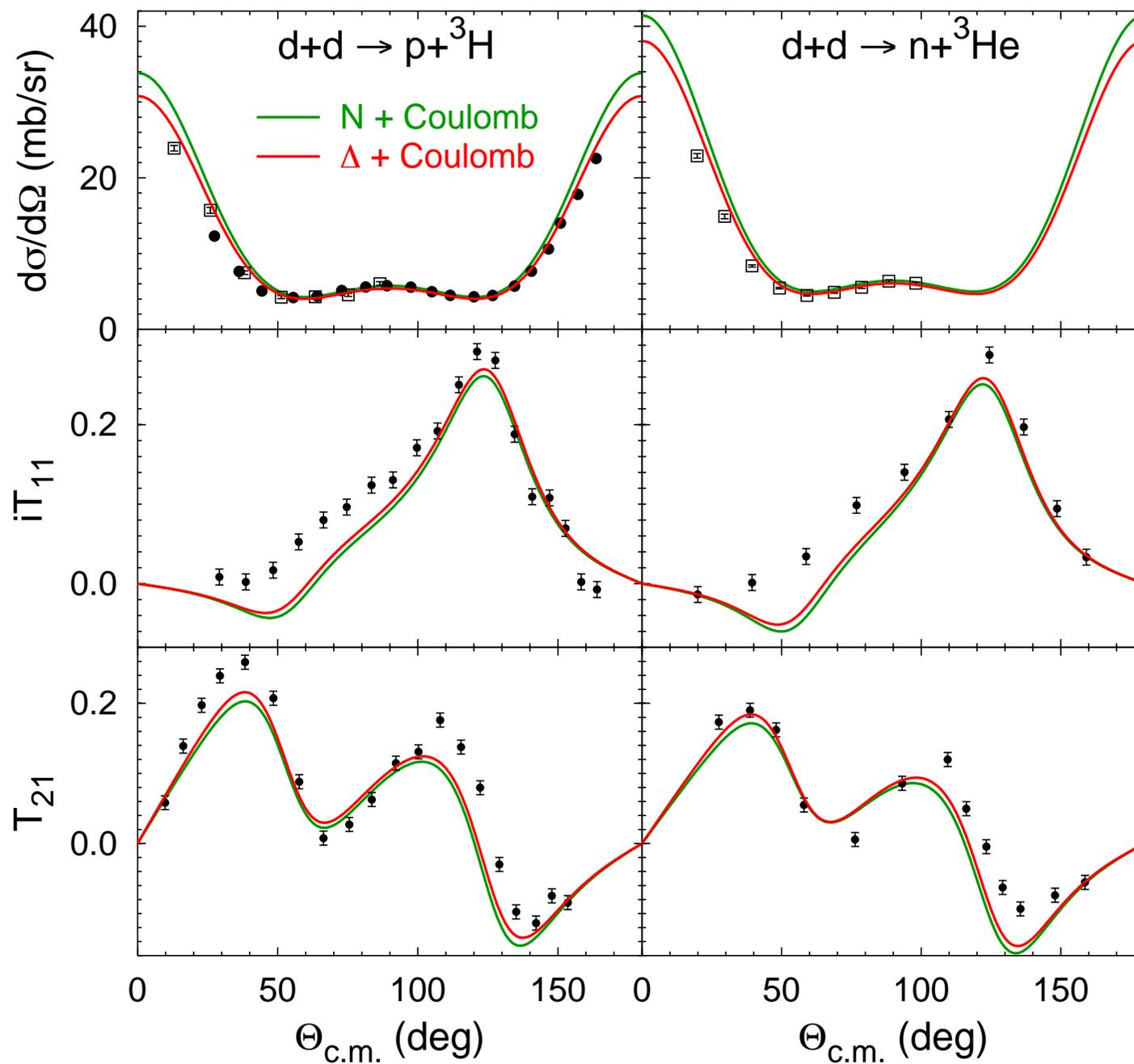
colour coding of results

CD Bonn + Δ	}	Coulomb effect
CD Bonn + Δ + Coulomb		
CD Bonn + Coulomb	}	3N force effect

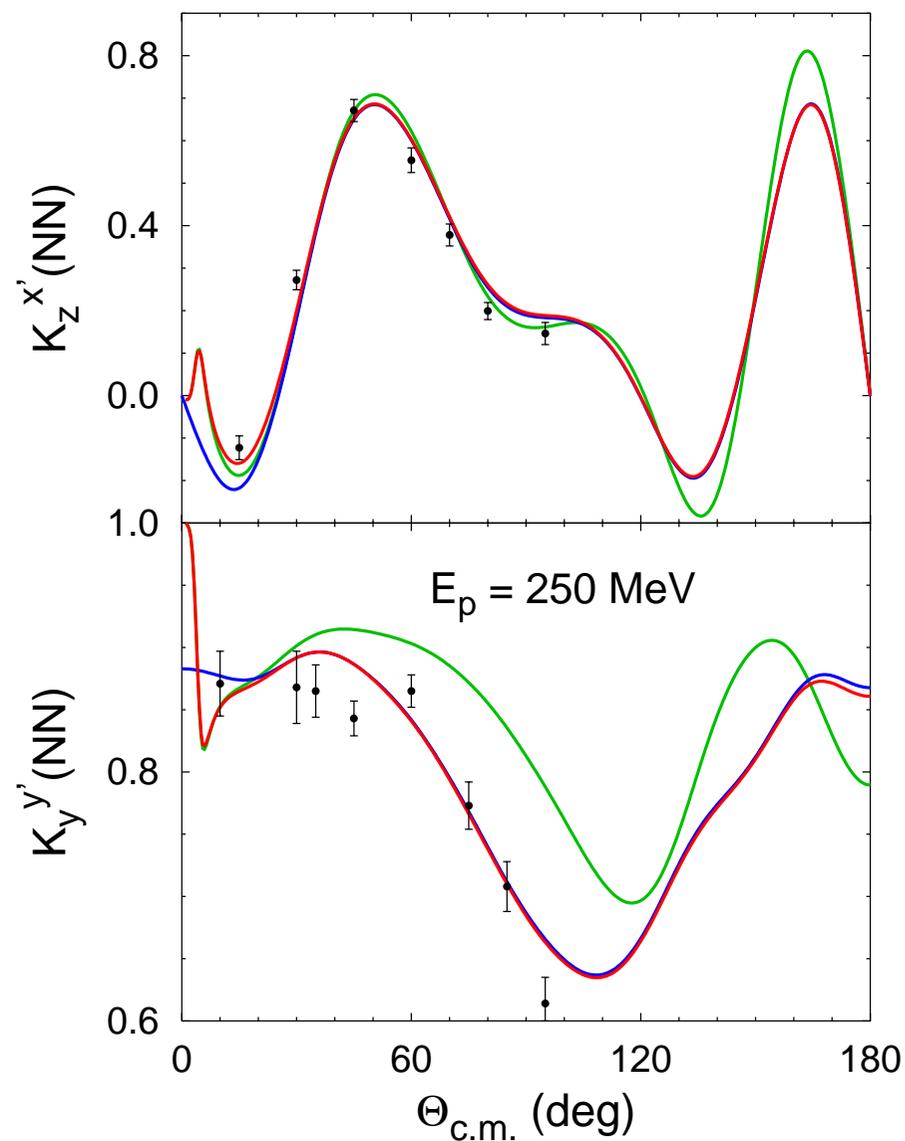
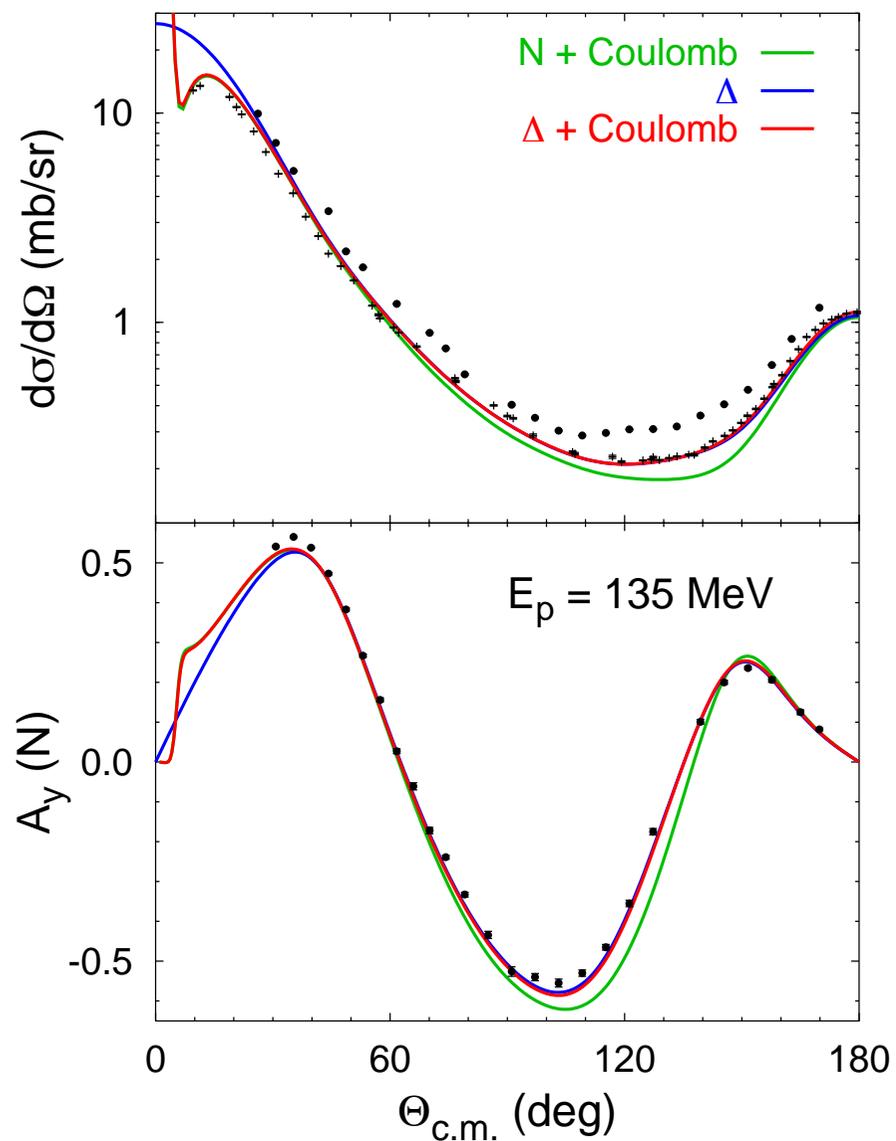
pd elastic scattering at low energies



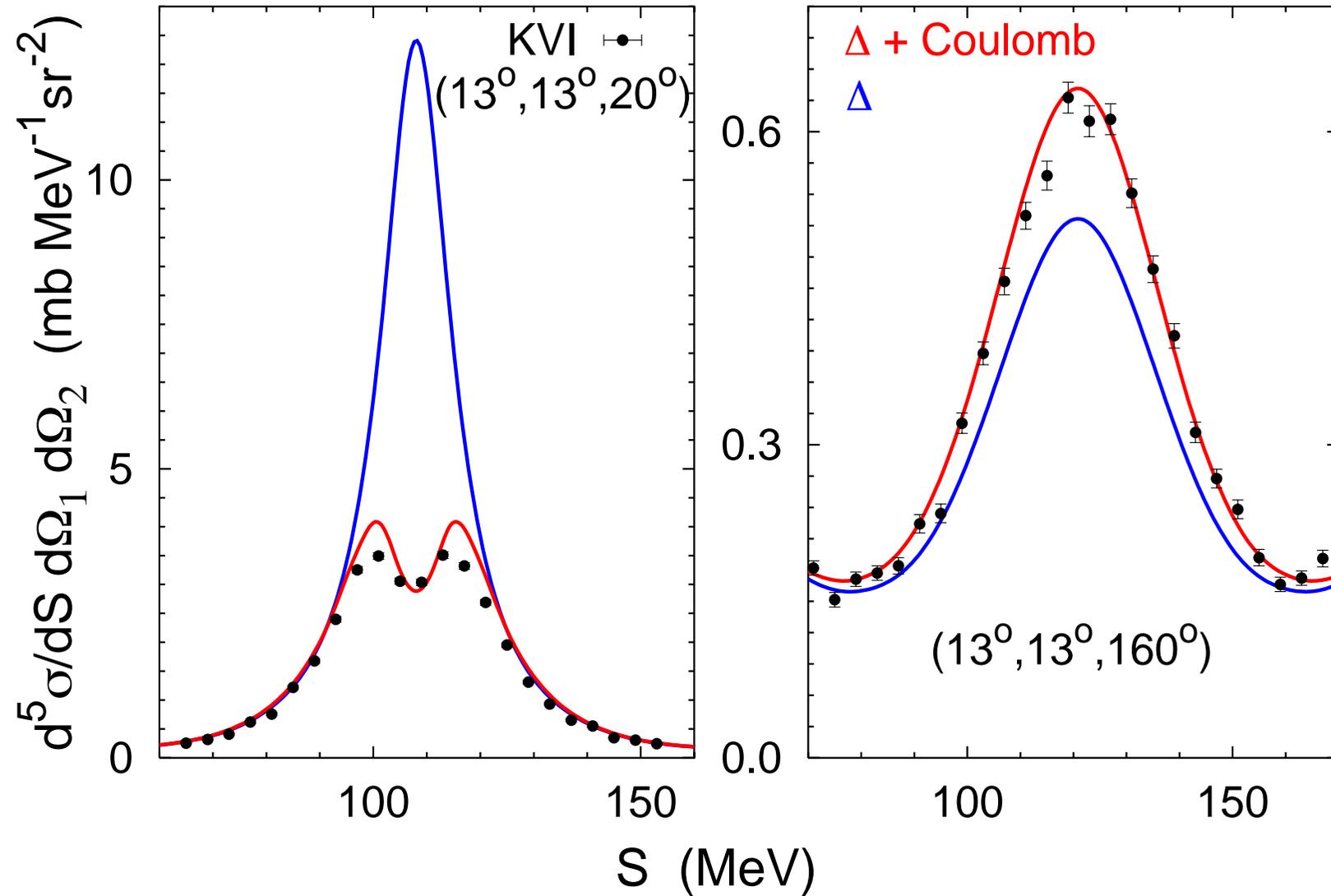
$d + d \rightarrow N + [3N]$ transfer at $E_d = 3$ MeV



pd elastic scattering at higher energies



dp breakup at $E_d = 130$ MeV



What Have We Learnt?

Already 40 Years ago, before the Advent of Dedicated Research on Few-Nucleon Systems:

Bethe: *Never in history before was so much research energy ever spent on one scientific problem as on the two-nucleon interaction.*

What Have We Learnt?

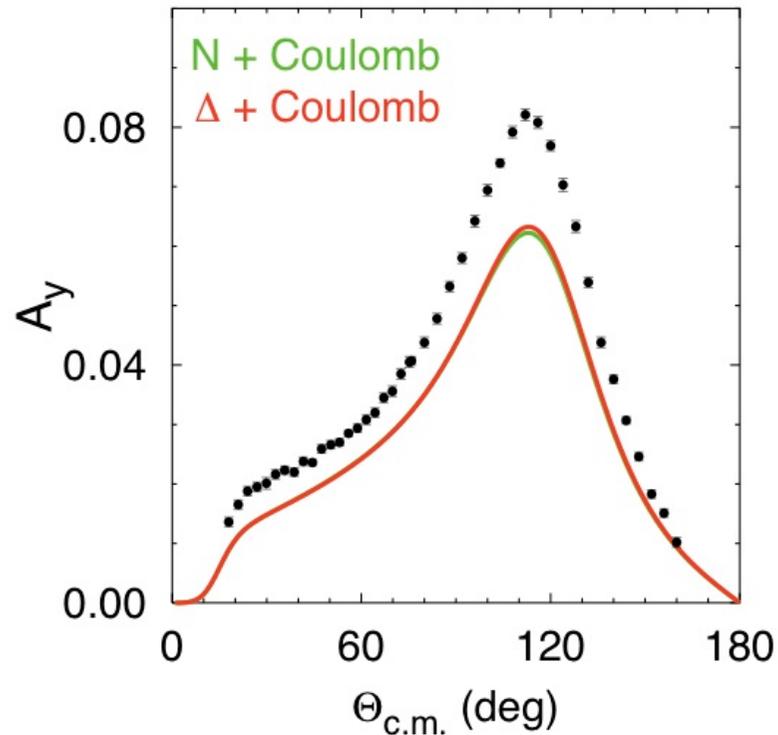
After 40 Years Research on Few-Nucleon Systems:

- large amount of 3N and 4N observables described well, Coulomb can be important
- 3N force needed for theoretical description of
 - bound states
 - thresholds and resonances in 4N scattering
 - 3N and 4N scattering at higher energies
- 4N force effects much smaller than 3N force effects
- despite successes, remaining questions

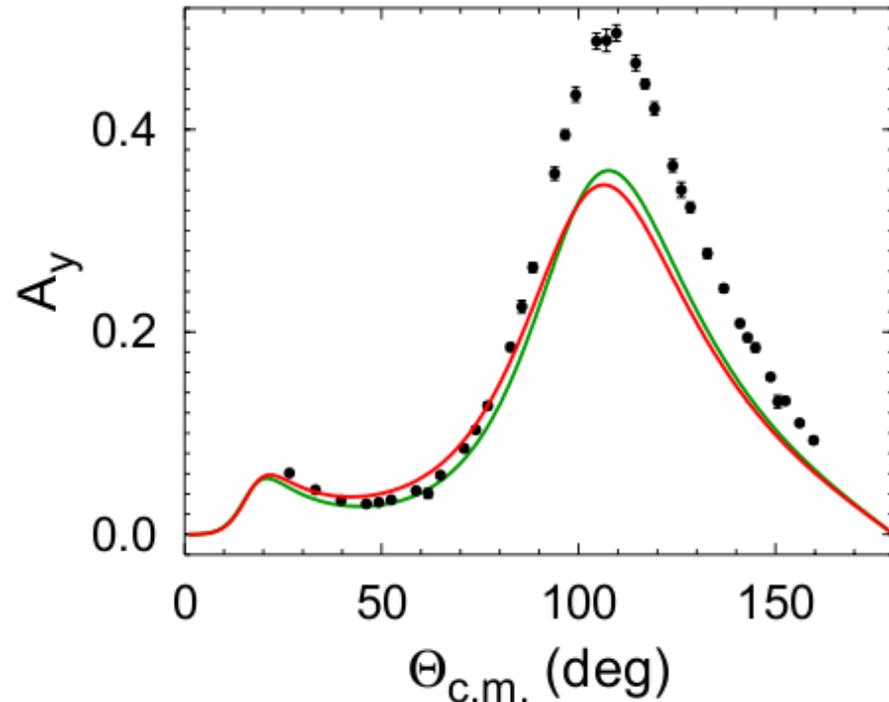
Remaining Questions

- discrepancies experiment/theory at low energies without clear hints for explanation: puzzles???

A_y problem in 3N and 4N scattering

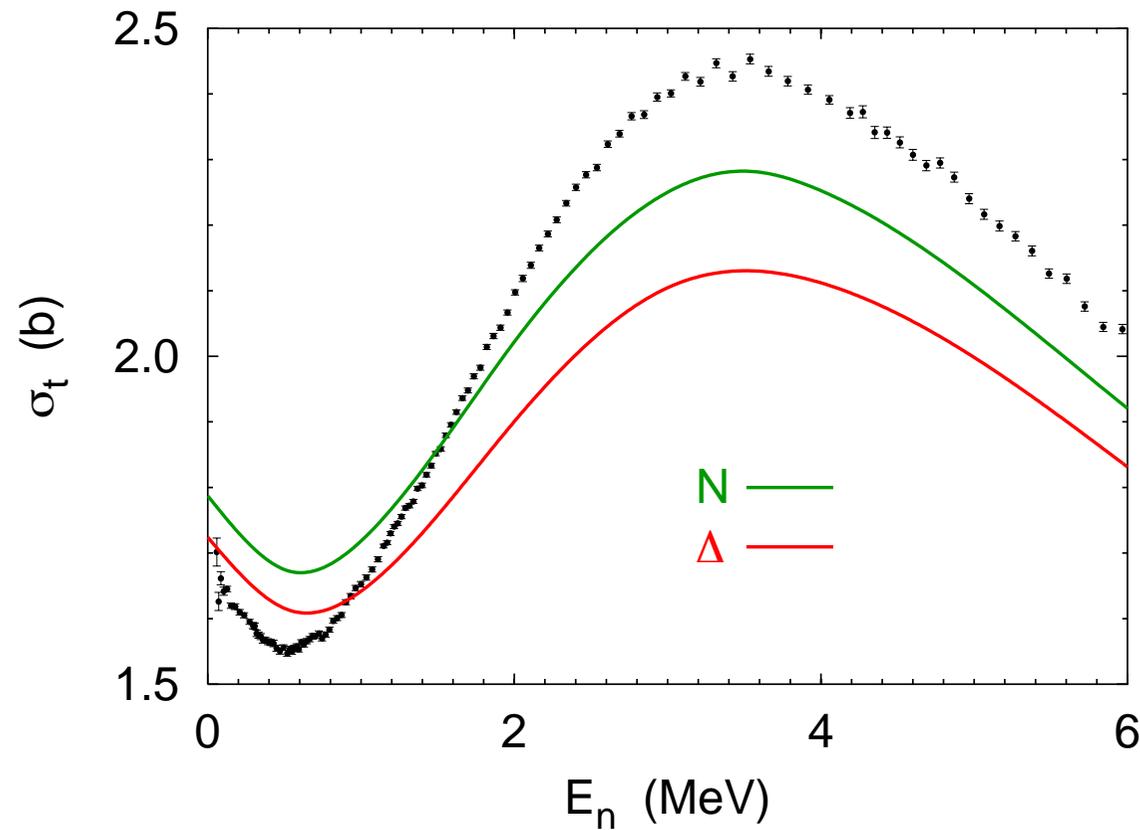


pd elastic scattering
 $E_p = 5$ MeV



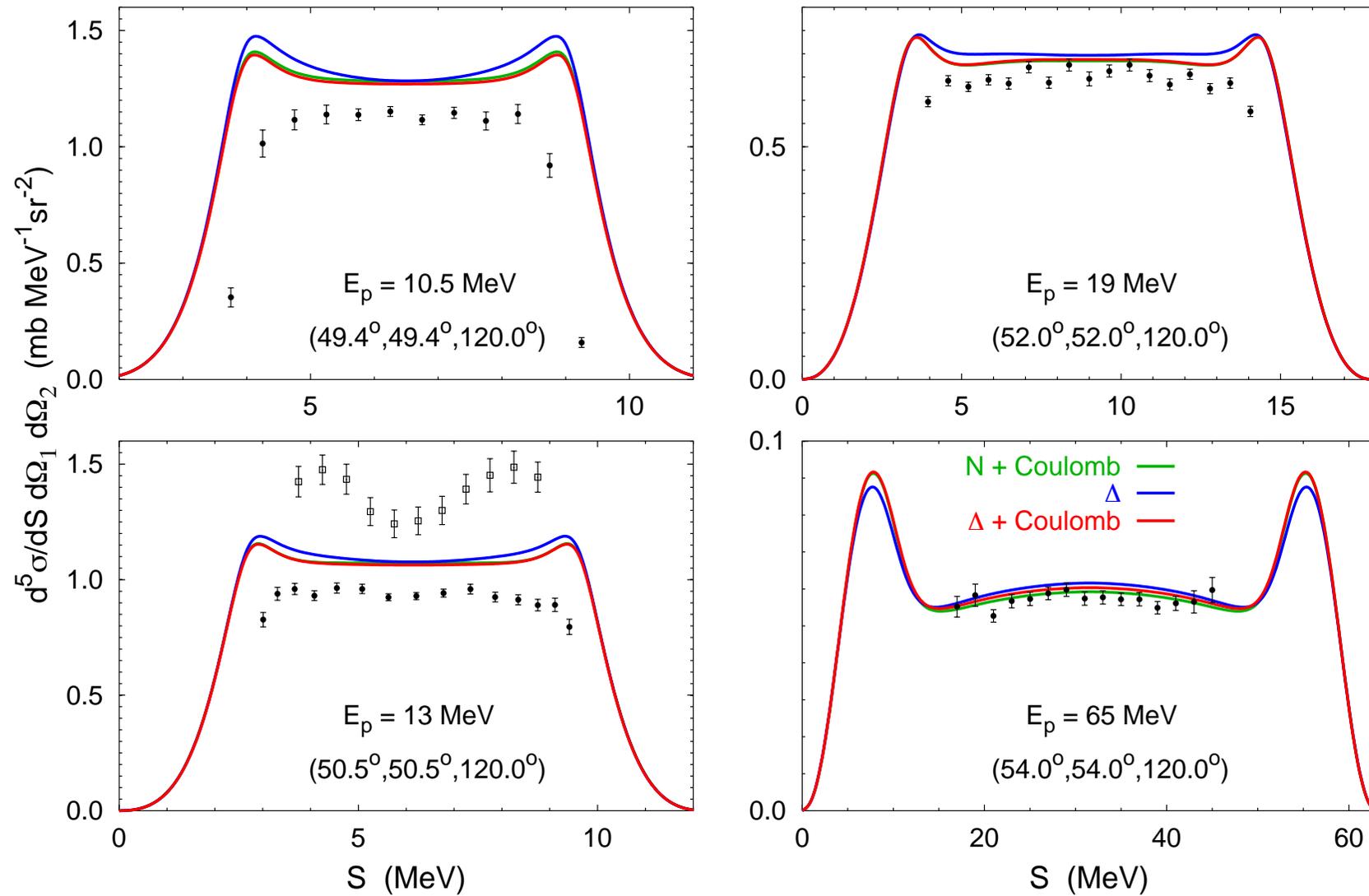
p^3He elastic scattering
 $E_p = 5.54$ MeV

problem of total $4N$ cross sections



n^3H elastic scattering

problem of Nd breakup: space-star anomaly

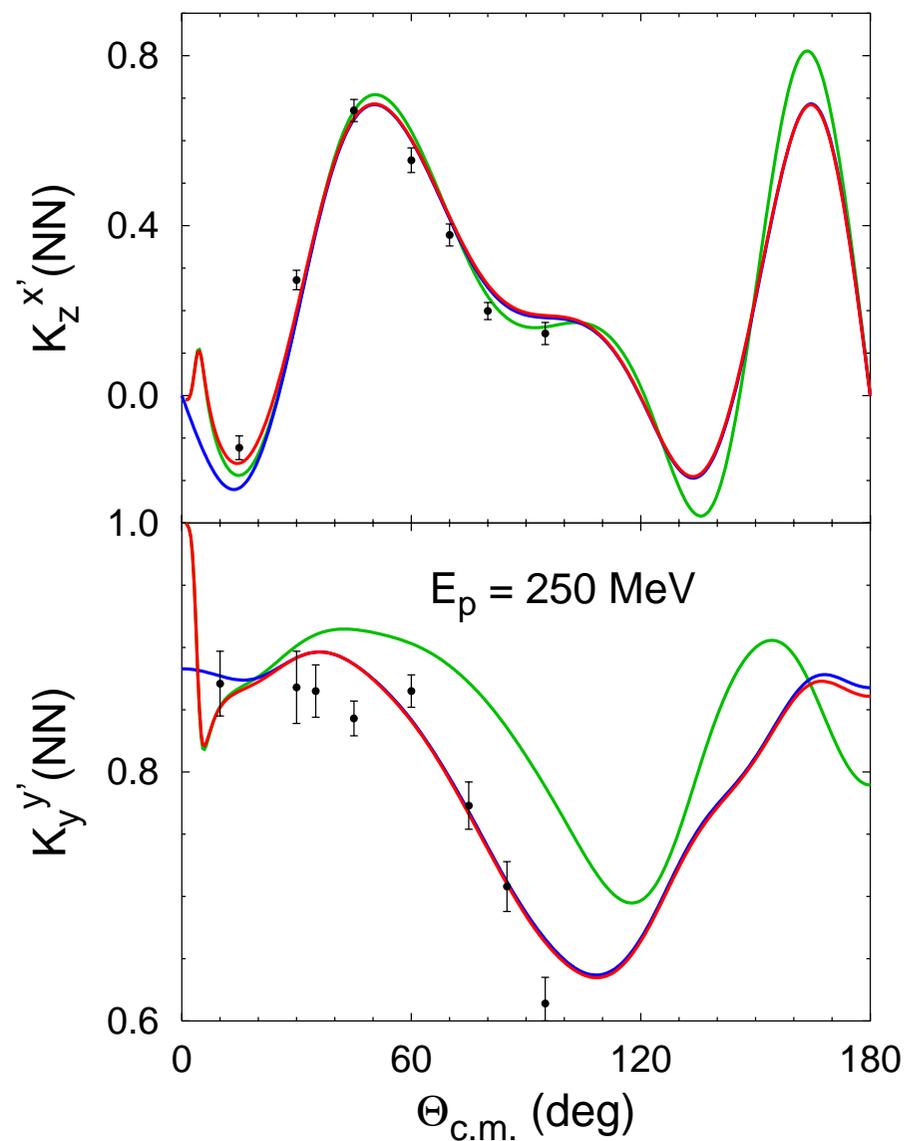
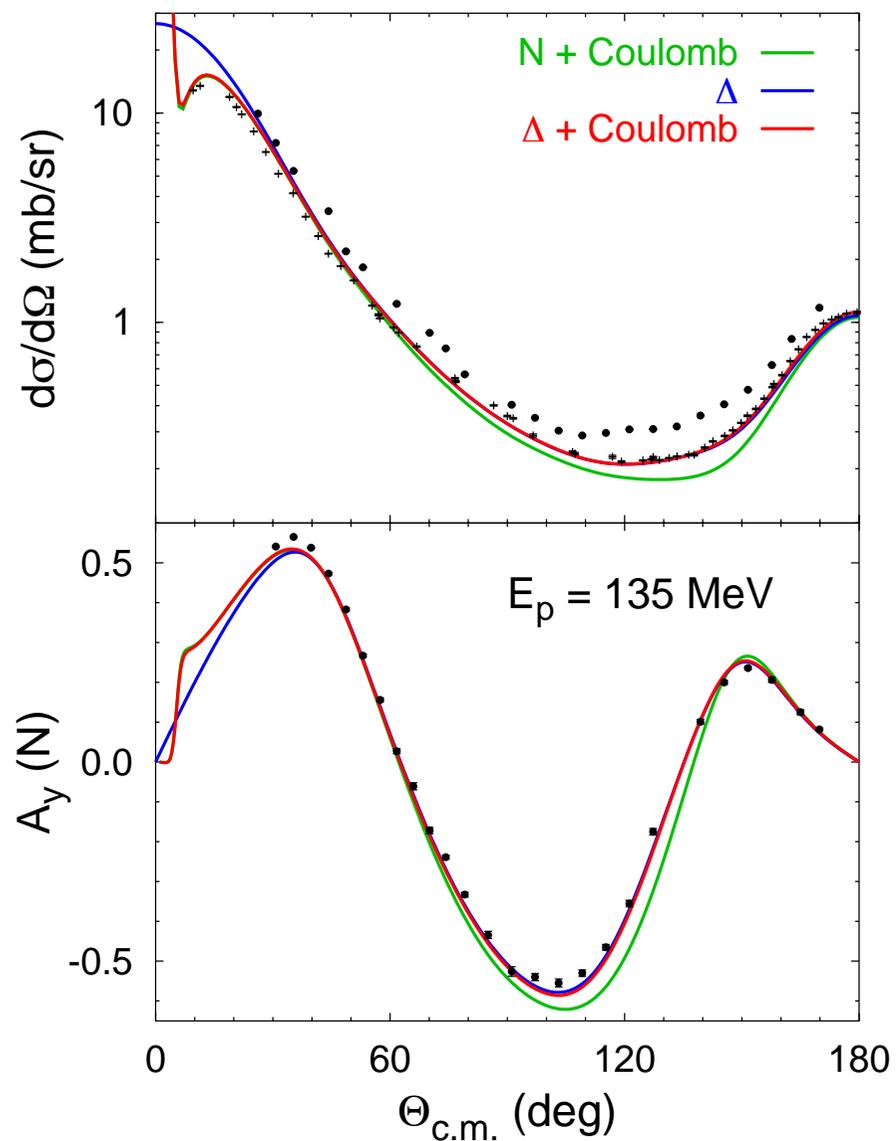


puzzle: large charge asymmetry?

Remaining Questions

- discrepancies experiment/theory at low energies without clear hints for explanation: puzzles???
- what is kinematics, what dynamics in the structure of observables?

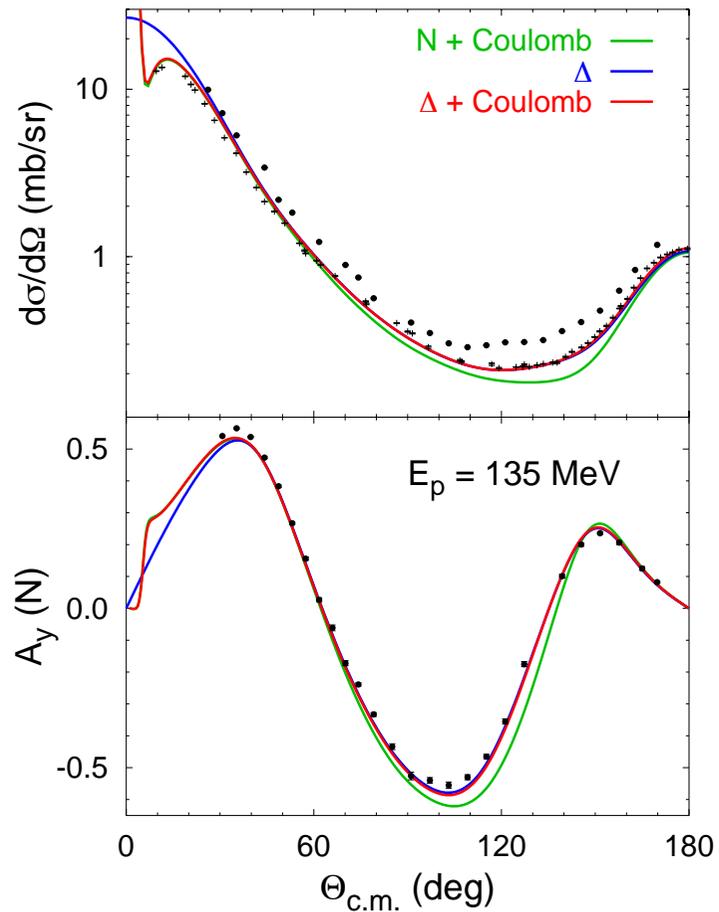
pd elastic scattering at higher energies



Remaining Questions

- discrepancies experiment/theory at low energies without clear hints for explanation: puzzles???
- what is kinematics, what dynamics in the structure of observables?
- how to ensure consistency of experimental data?

pd elastic scattering at higher energies



two inconsistent data sets in *pd* elastic scattering
in 2N scattering inconsistent data can be removed, NOT in 3N scattering

Remaining Questions

- discrepancies experiment/theory at low energies without clear hints for explanation: puzzles???
- what is kinematics, what dynamics in the structure of observables?
- how to ensure consistency of experimental data?
- how to extract detailed properties of many-nucleon forces from few-nucleon data?

Few-Nucleon Systems:

Testing OR Tuning Nuclear Dynamics?

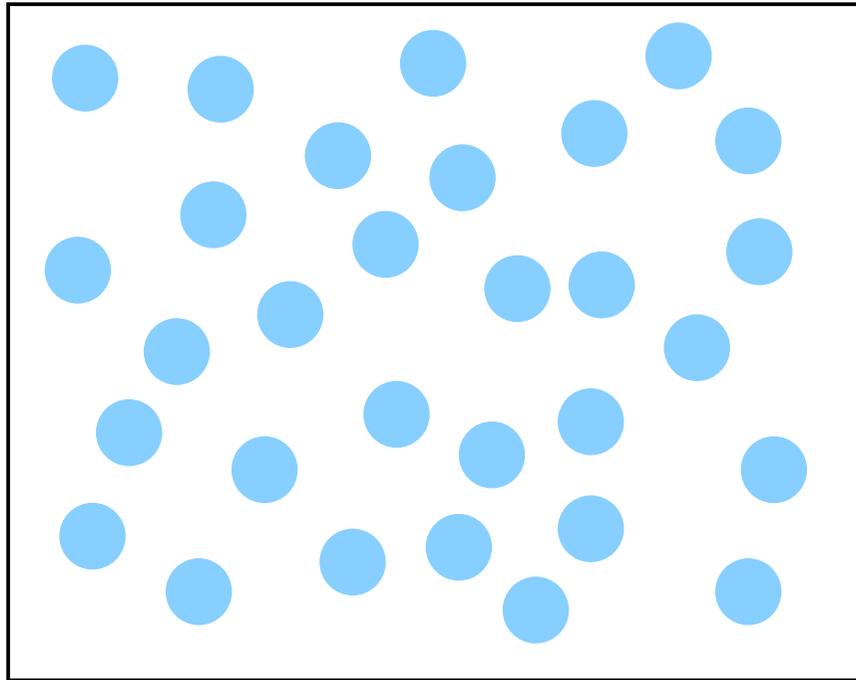
ab initio OR *ab exitu*?

The Beautiful Bridges of Iowa



Bridge between Nuclear Structure and Few-Nucleon Systems?

Quantum Optics

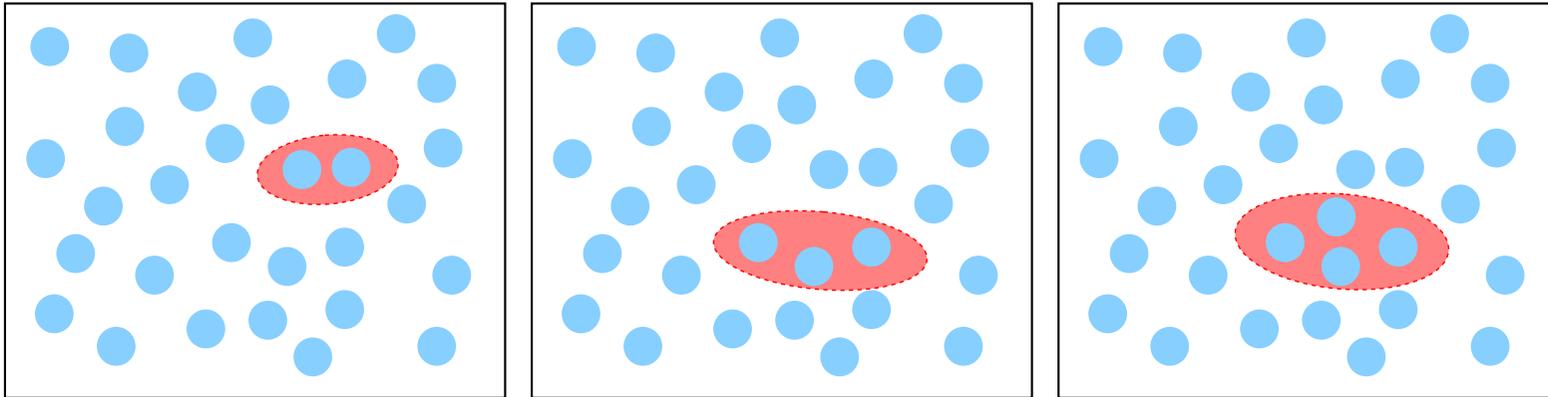


Atoms in Trap:

Atoms Move Freely Except for Trap Boundaries -

Reactions as in Free Space

Atoms in Trap



Reaction Rates: Loss of Atoms from Trap

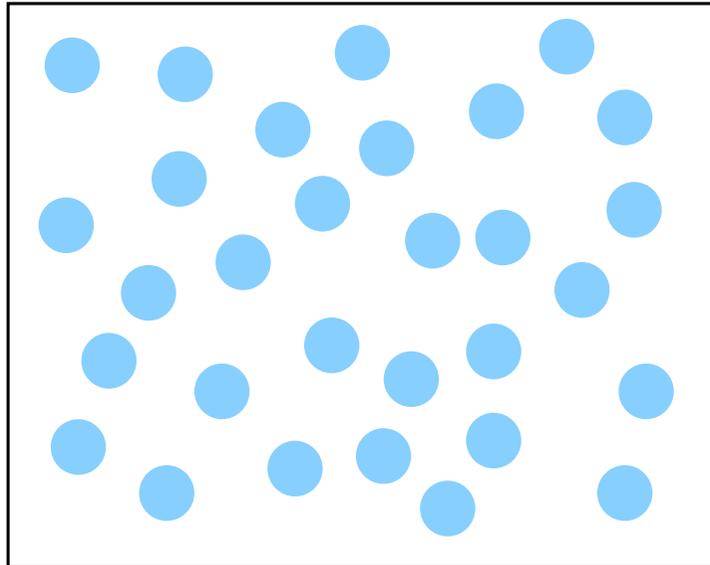
2A Reaction

3A Reaction

4A Reaction + ?

Loss by Forming Bound States

What is Special about Few-Body Reactions in Cold Atoms?



Interactions between

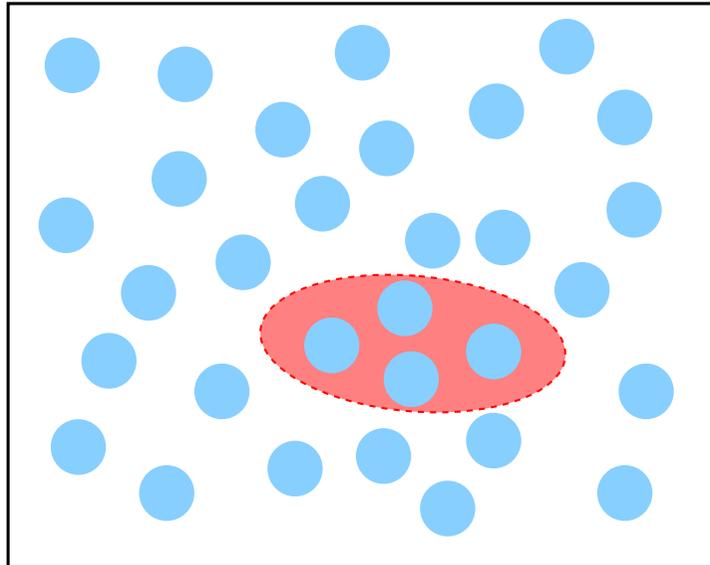
Atoms

Nucleons

Known and Tunable
Tunable to Efimov Regime
Strong

Partially Unknown, but Fixed
Weak

What is Special about Few-Body Reactions in Cold Atoms?



Reactions with
Atoms Nucleons

An Example - Time-Reversed Reactions - Calculations by Deltuva





Dear James, best wishes for a further successful future,
wherever you may be!