





Nuclear Forces from Lattice Quantum Chromodynamics

Martin J. Savage University of Washington International Conference on Nuclear Theory in the Supercomputing Era - 2013 Iowa, May 2013



Me and James : **197.327**



Caltech 1985-86



James : Visiting Professor

Me : first year grad student

Computer : big old VAX

Result : I know **ħc** !





The Structure and Interactions of Matter from QCD





 $\Lambda_{\rm QCD}$



 α_e

Small number of input parameters responsible for all of strongly interacting matter



The Road from QCD







Fine-Tunings define our Universe







Parameter/Gauge Landscape

- Nuclear physics exhibits fine-tunings
 - Why ??
 - Range of parameters to produce sufficient carbon ?
- Need to calculate over a range of parameters to disentangle the chiral nuclear forces anyway!



Organizing Nuclear Forces



Effective Field Theory introduced by Weinberg in the early 1990's to systematize nuclear forces

- Low-energy EFT of QCD
- Chiral symmetries of QCD
- Quark mass dependence
- Interesting RG behavior
- Softer Interactions
 V_{lowk} , SRG
- Organization of multi-nucleon forces

	2N force	3N force	4N force
LO	X + -+	—	
NLO	X 🔤 🕅		
N ² LO	 ⊂ <	+++ +-¥ X	
N ³ LO		<u> 4 </u> ; -	 / / 6



Chiral Interactions in Nuclear Calculations

	25 force	3N force	4N force
1.0	ΧН	-	_
NLO	X 비서 비비	-	_
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N'LO	현서년 성원X-	₩₩-	114-

No-Core Shell Model Calculations with Chiral Forces



Experiments constrain counterterms leading to predictions for other observables at a given order in the EFT expansion



Refining Nuclear Forces and Multi-Nucleon Interactions: Enhancing Predictive Capabilities





iii) Number of counterterms for required level of precision

iii) and/or direct calculation of desired quantity



Lattice QCD



Monte-Carlo Evaluation of QCD Path Integral



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Not Quite QCD !

Lattice Spacing : Lattice Volume : $a \ll 1/\Lambda \chi$

 $m_{\pi}L >> 2\pi$

(Nearly Continuum)

(Nearly Infinite Volume)

Systematically Extrapolate to QCD Effective Field Theory gives form of extrapolation a = 0 and $L = \infty^{\circ}$



Gauge Field Configurations The Vacuum is Complex







Topological Charge Density (Massimo DiPierro)



 $\Delta t \sim 6 \times 10^{-24} \ s$

"Pixelation" ~ (0.12 x 10⁻¹⁵ m)³



Quark Propagator on One Gauge Configuration

Pion, Nucleon from same propagators

Quark Propagators Quarks and Gluons are Confined (T=0)





Cancellation of

Probability Amplitudes







US Lattice Quantum Chromodynamics

















Misson-critical, custom logic (hatched) for high-performance memory access and fast, low-latency off-node communications is combined with standards-based, highly integrated commercial library components.



á bacada



capacity

Cold Nuclear Physics









Masses of the Particles









• $< X^n >$

Structure of the Nucleon





g_A and other q²=0 matrix elements

charge and magnetic radii, etc

associated form factors

First calculations at physical pion mass during 2012

Precision is needed (complete uncertainty quantification)





Spectrum of the Hadrons





- Spectrum of mesons and baryons
 - exotics, molecules
 - coupled channels, etc
 - provided motivation for 12 GeV upgrade





Lattice QCD will predict the exotic spectrum before or during the GlueX experiment (with sufficient compute resources)



Fundamental Interactions







Non Resonant Phase Shifts I=2 pion-pion







Resonant Phase Shifts I=1 pion-pion







ρ- resonance successfully determined



NN Interactions





Deuteron appears to be unnatural but not finely-tuned ?? Generic feature of YM with n_f=3



Nuclei







Deuteron







Helium















Roadblocks of the Past





Contractions - 2012 no longer an issue for light nuclei

e.g. He-4 : 0.8 core-seconds per time-slice Orginos+Detmold algorithm



Signal to noise

Large numbers of measurements





Hyperon Nucleon Interactions



Meissner+Haidenbauer - Experiment + YN-EFT (LO) 60 2050 10 (degrees) 00 00 0 -10 -20 Ś Ø 20 -30 NSC97f Juelich '04 NSC97f -40 EFT 10 Juelich '04 -50 -60<u>∟</u> 0 100 200 300 400 500 100 200 300 400 500 p_{LAB} (MeV) ${\rm p}_{\rm LAB}~({\rm MeV})$

> Cancellation between channels in dense matter energy-shift of hyperon



Hyperon Nucleon Interactions



NPLQCD - Lattice QCD + YN-EFT (LO)



Cancellation between channels in dense matter energy-shift of hyperon



Future Cold Nuclear Physics Program : Physical Pion Mass usoco





Tuesday, May 14, 2013

Contributions to nucleon spin

USQCD Proposed Production 2014-2019



5	Ð	e	DH
 $\mathbf{\nabla}$	Co.	$\mathbf{\nabla}$	

$N_{c}^{3} \times N_{t}$	Action		m_{π}	$m_{\pi}L$	$m_{\pi}T$	Traj.	Configs.	Str-A	Str-B	HSp	HI
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$48^3 \times 96$	DWF	0.110	140	3.9	7.8	$5 imes 10^3$		28	360^{\dagger}		
$64^3 \times 128$	DWF	0.086	140	3.9	7.8	$5 imes 10^3$		64	844^{\dagger}		

Assume current funding levels throughout period - NP 50% partner



Beyond Computational : Formal Issues



- What Lattice QCD calculations are required to predict multi-body nuclear reactions ?
 - Coupled channels extension of Luscher underway

Nuclear Reactions from Lattice QCD Briceno, Davoudi, Luu http://www.int.washington.edu/PROGRAMS/13-53w/



- How to optimally match to nuclear many-body technology ?
 - do we simply pass along energy eigenvalues ?



Collaboration is Crucial







LQCD Codes on the Latest Hardware







Closing Remarks





Lattice QCD, combined with chiral EFT and nuclear many-body techniques, will provide first principles predictive capabilities for Nuclear Physics

Enable calculations with **quantifiable uncertainties** of the nuclear forces and of processes occurring in nuclei and astrophysical environments where experiments are not possible.

Matching to nuclear many-body machinery is beginning



Happy Birthday James









THE END