

Predictions for nuclear rotational structure from *ab initio* calculations

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Nuclear Theory in the Supercomputing Era
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Rotational structure from *ab initio* nuclear theory?

Ab initio theory should be able to describe nuclei

Light nuclei display rotational band structure

\therefore *Ab initio* theory should be able to predict rotational bands

But... Convergence challenges in calculation of relevant observables

– **Qualitative emergence** of rotational “features”?

Rotational energies, rotational transition patterns

– Robust **quantitative prediction** of rotational observables?

Rotational energy parameters, intrinsic E2 matrix elements

– Physical nature of rotation in light nuclei — What can we learn?

Emergence of rotational patterns in Be isotopes

M. A. Caprio, P. Maris, and J. P. Vary, Phys. Lett. B **719**, 179 (2013).

P. Maris, M. A. Caprio, and J. P. Vary, Phys. Rev. C **91**, 014310 (2015).

C. W. Johnson, Phys. Rev. C **91**, 034313 (2015).

M. A. Caprio, P. Maris, J. P. Vary, and R. Smith, Int. J. Mod. Phys. E **24**, 1541002 (2015), [arXiv:1509.00102](https://arxiv.org/abs/1509.00102).

Separation of rotational degree of freedom

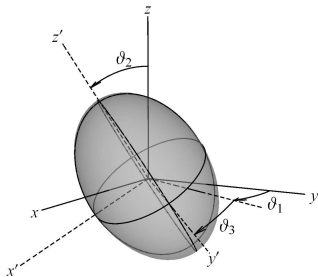
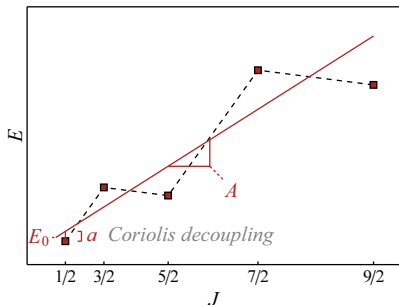
Intrinsic state $|\phi_K\rangle$ & rotation in Euler angles ϑ ($J = K, K+1, \dots$)

$$|\psi_{JKM}\rangle \propto \int d\vartheta \left[\mathcal{D}_{MK}^J(\vartheta) |\phi_K; \vartheta\rangle + (-)^{J+K} \mathcal{D}_{M-K}^J(\vartheta) |\phi_{\bar{K}}; \vartheta\rangle \right]$$

Rotational energy

$$E(J) = E_0 + A \left[J(J+1) + \underbrace{a(-)^{J+1/2} \left(J + \frac{1}{2} \right)}_{\text{Coriolis } (K=1/2)} \right] \quad A \equiv \frac{\hbar^2}{2\mathcal{I}}$$

Rotational relations on electromagnetic transitions ($E, M1, \dots$)



Observed energy levels for $A = 7$ nuclei

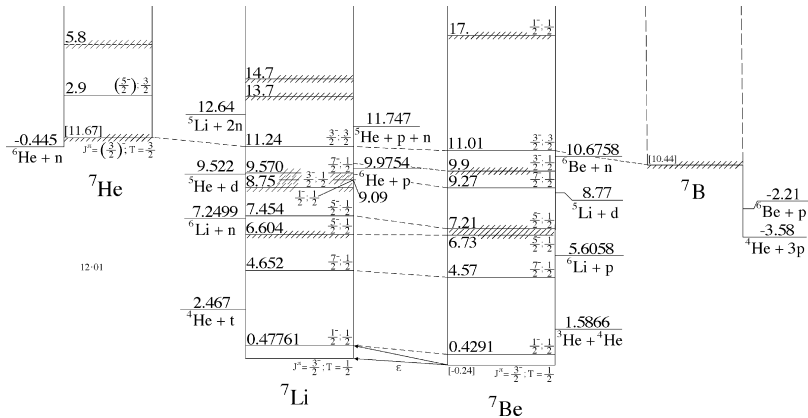
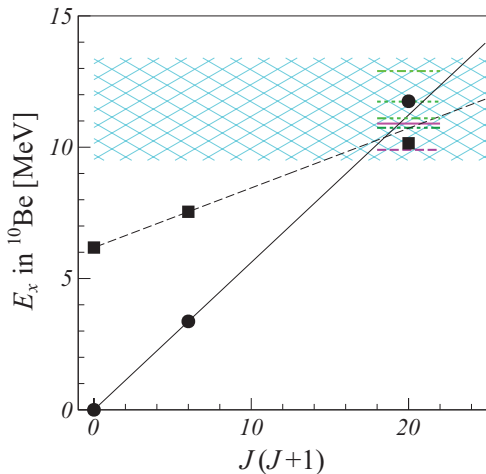


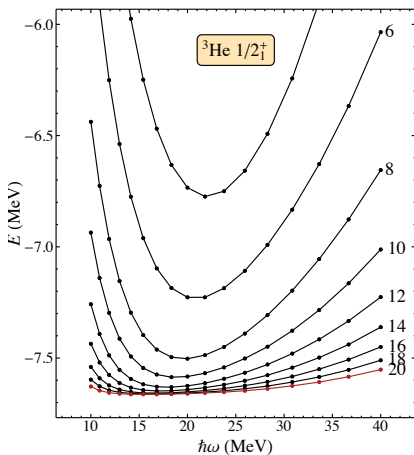
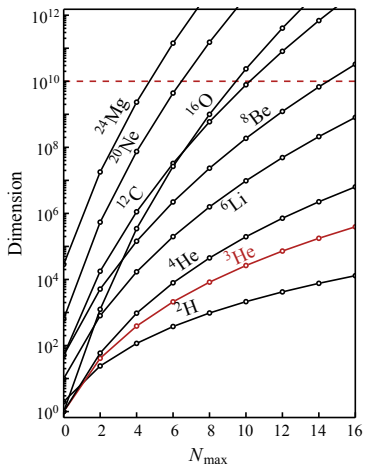
Figure from D.R. Tilley *et al.*, Nucl. Phys. A **708**, 3 (2002).

Yrast and excited bands in ^{10}Be

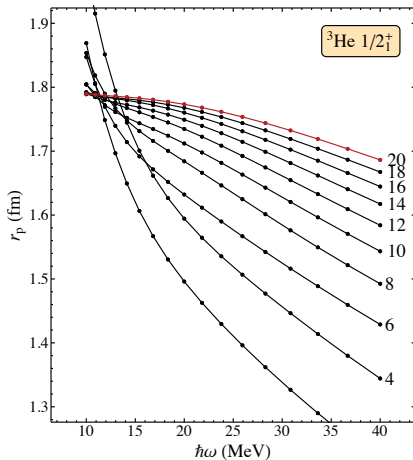
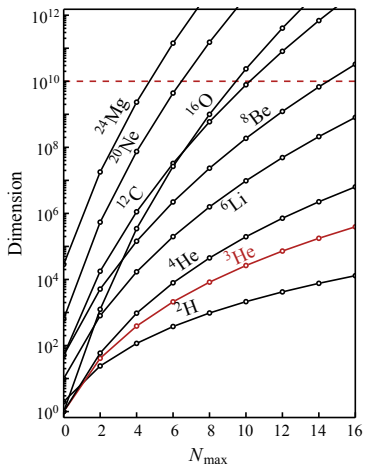


From D. Suzuki *et al.*, Phys. Rev. C **87**, 054301 (2013). Orbital schematics from Y. Kanada-En'yo, H. Horiuchi, and A. Doté, Phys. Rev. C **60**, 064304 (1999).

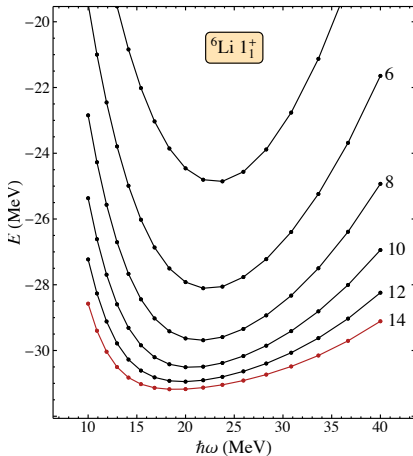
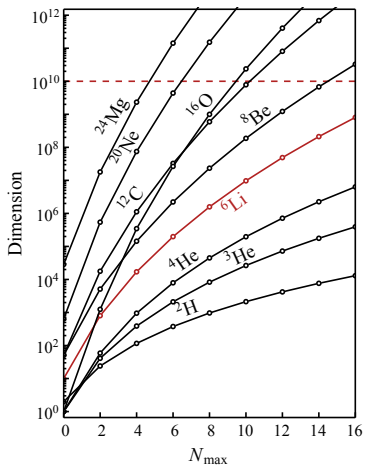
Convergence of NCCI calculations



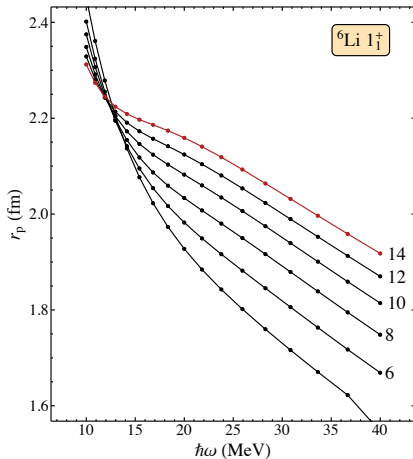
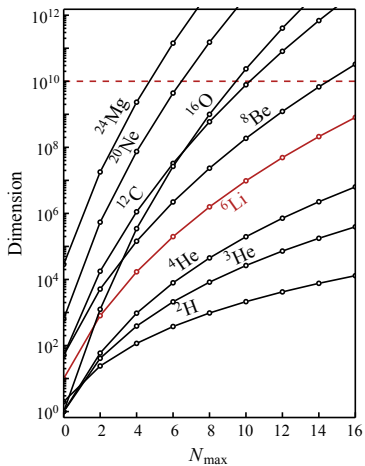
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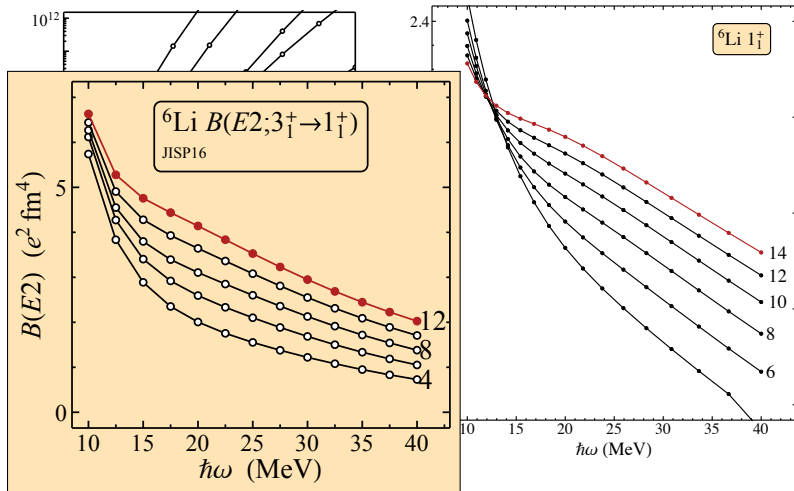
Convergence of NCCI calculations



Convergence of NCCI calculations



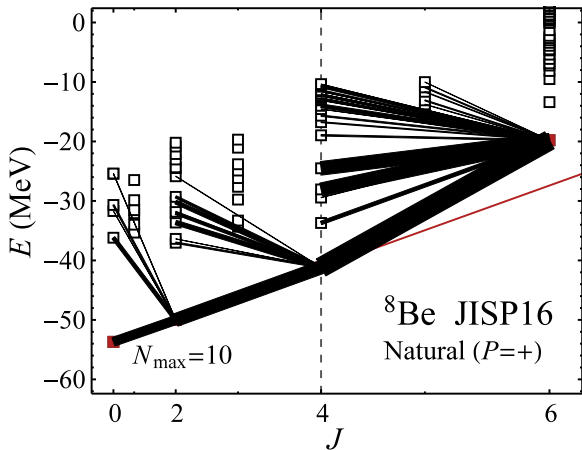
Convergence of NCCI calculations



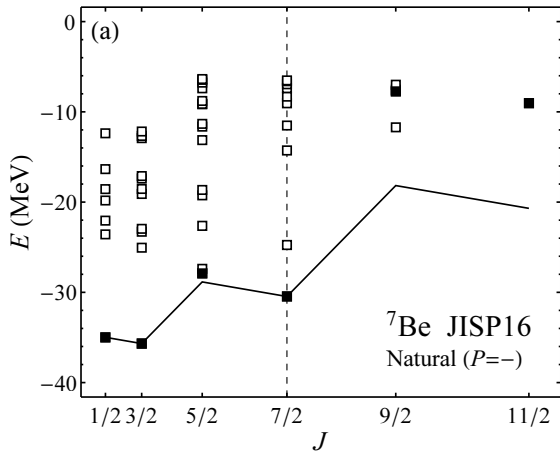
The ^8Be yrast band

Shell model: Valence space angular momentum $J \leq 4$

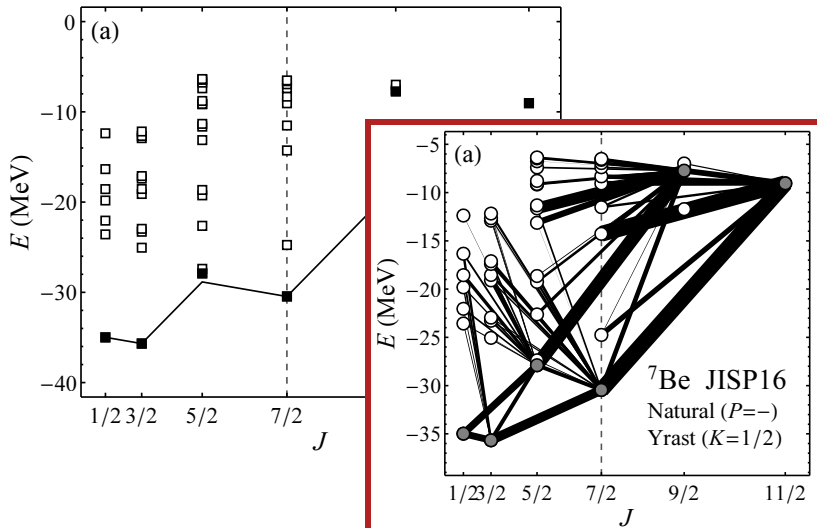
Cluster model: Molecular rotation of $\alpha + \alpha$ dimer



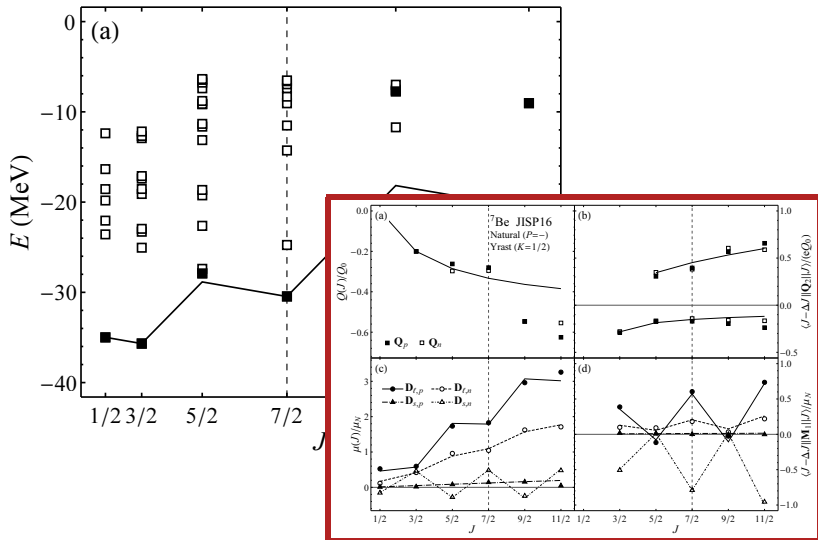
Yrast $K = 1/2$ rotational band in ${}^7\text{Be}$



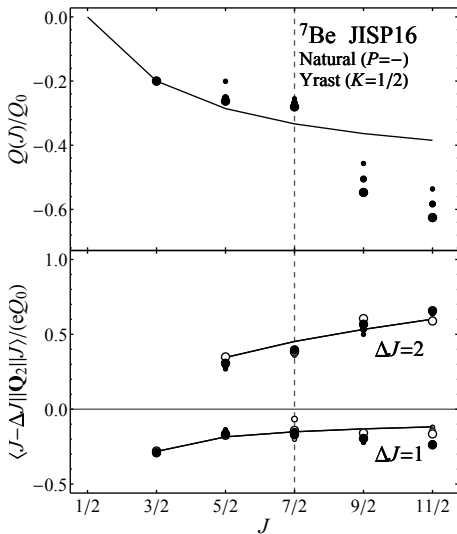
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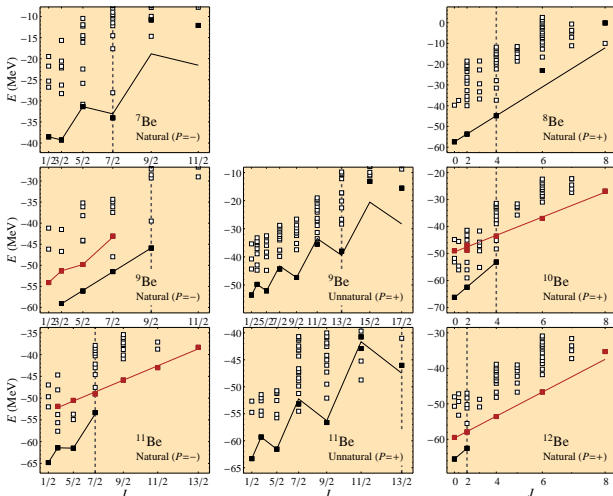
Yrast $K = 1/2$ rotational band in ${}^7\text{Be}$



Convergence of in-band transition matrix elements

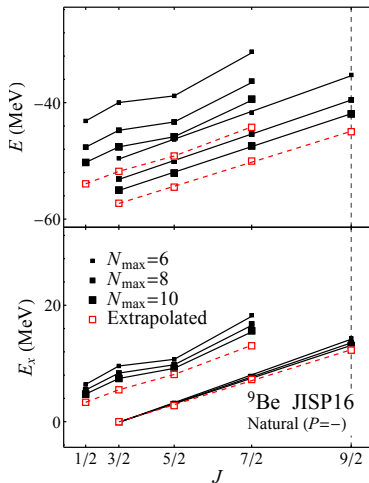
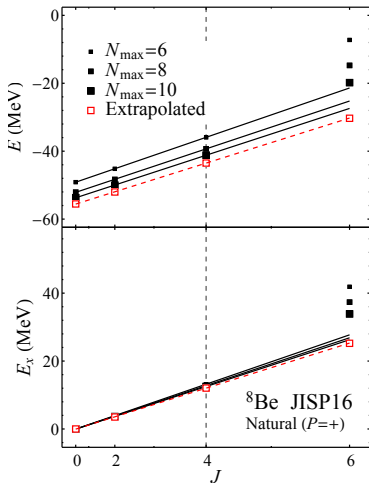


Rotational bands in ${}^7\text{-}^{12}\text{Be}$ from NCCI calculations

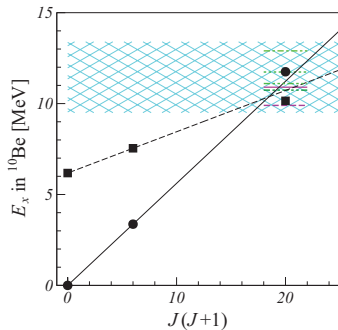
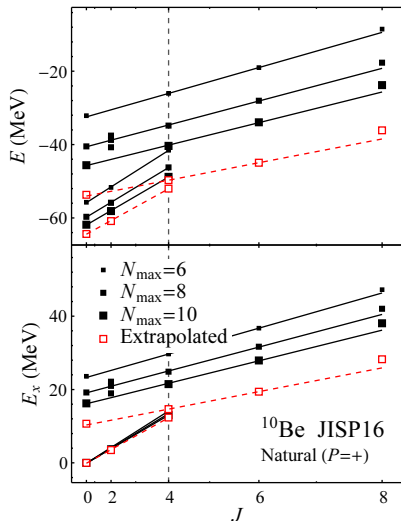


M. A. Caprio, P. Maris, and J. P. Vary, Phys. Lett. B **719**, 179 (2013).
 P. Maris, M. A. Caprio, and J. P. Vary, Phys. Rev. C **91**, 014310 (2015).

Convergence of energies for band members



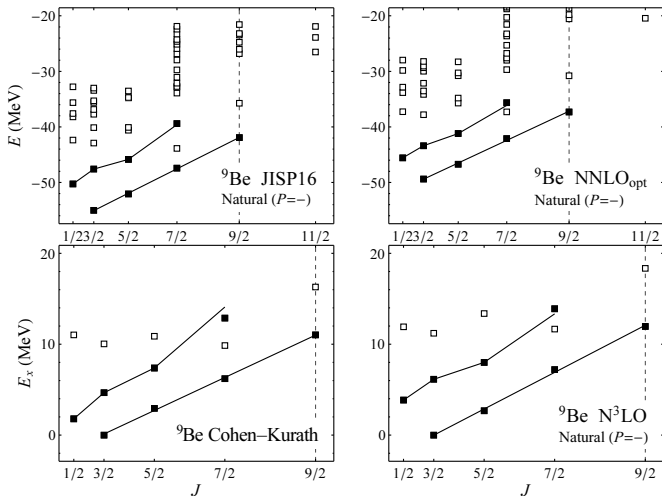
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From D. Suzuki *et al.*, Phys. Rev. C **87**, 054301 (2013).

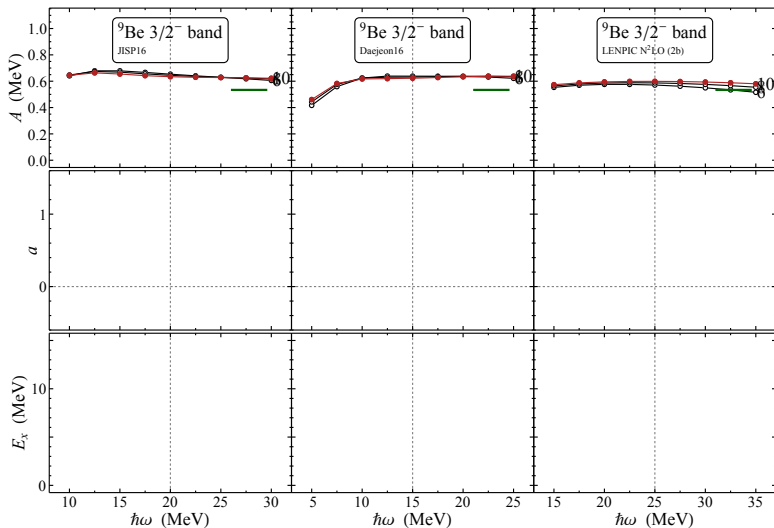
Extrapolation: Exponential in N_{\max} (3-point); see
 P. Maris, J. P. Vary, and A. M. Shirokov, Phys. Rev. C
79, 014308 (2009).

Rotational structure in ${}^9\text{Be}$ across interactions



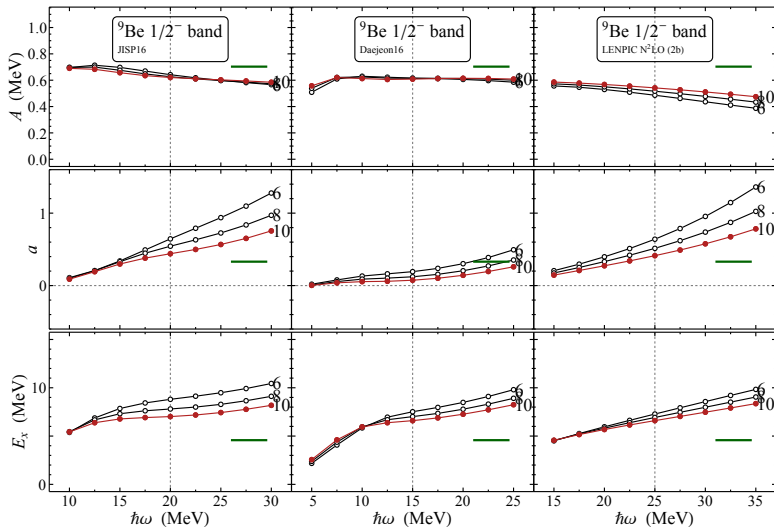
Calculations for Cohen-Kurath and N³LO from C. W. Johnson, Phys. Rev. C **91**, 034313 (2015).

Convergence of band parameters?



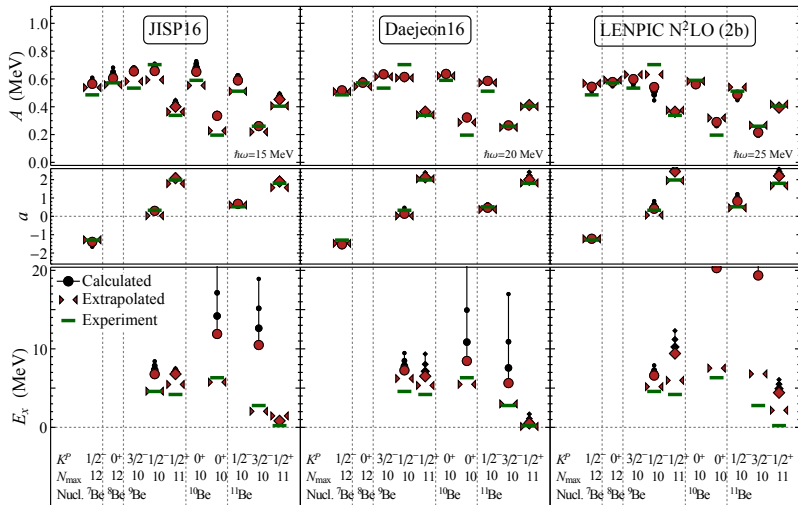
Band parameters obtained from energies of three lowest band members

Convergence of band parameters?

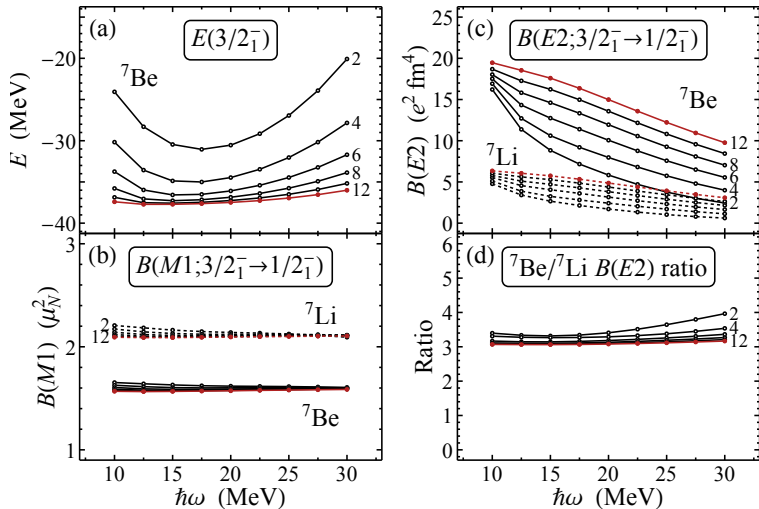


Band parameters obtained from energies of three lowest band members

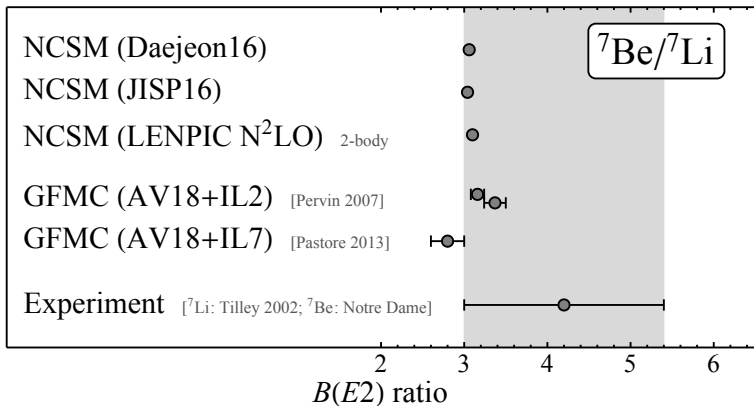
Ab initio rotational band parameters for Be isotopes



Convergence of $B(E2)$'s and their *ratio* for ${}^7\text{Be}/{}^7\text{Li}$



Comparison of calculated $E2$ ratios for ${}^7\text{Be}/{}^7\text{Li}$



Summary

Can we predict nuclei *ab initio*?

Challenge: Computational scale explosion

Emergence of rotational patterns

M. A. Caprio, P. Maris, and J. P. Vary, Phys. Lett. B **719**, 179 (2013).

P. Maris, M. A. Caprio, and J. P. Vary, Phys. Rev. C **91**, 014310 (2015).

C. W. Johnson, Phys. Rev. C **91**, 034313 (2015).

M. A. Caprio, P. Maris, J. P. Vary, and R. Smith, Int. J. Mod. Phys. E **24**, 1541002 (2015), [arXiv:1509.00102](https://arxiv.org/abs/1509.00102).

Although energies & electromagnetic moments/transitions ($E2$) are unconverged...

Ratios of observables within a band can be robustly rotational

Robustness of rotational structure across interactions?

Quantitative agreement with experiment?

Underlying structure? *Rotational separation* vs. *nature of intrinsic state*

- Valence shell structure? e.g., SU(3) correlations
- Cluster structure? $\alpha + \alpha$ $\alpha + n + \alpha$ $\alpha + 2n + \alpha$...
- Symplectic multishell correlations?

Collaborators: Pieter Maris (ISU), James Vary (ISU), Patrick Fasano (ND)

