



東北大学

Experimental approach to three-nucleon forces via three- and four-nucleon scattering

Kimiko Sekiguchi

Department of Physics, Tohoku University

Sendai, JAPAN

Three-Nucleon Forces in Nucleus

Three-Nucleon Force (3NF)

key element to fully understand properties of nucleus.

- First evidence of 3NF : Binding Energies of Triton (^3H)



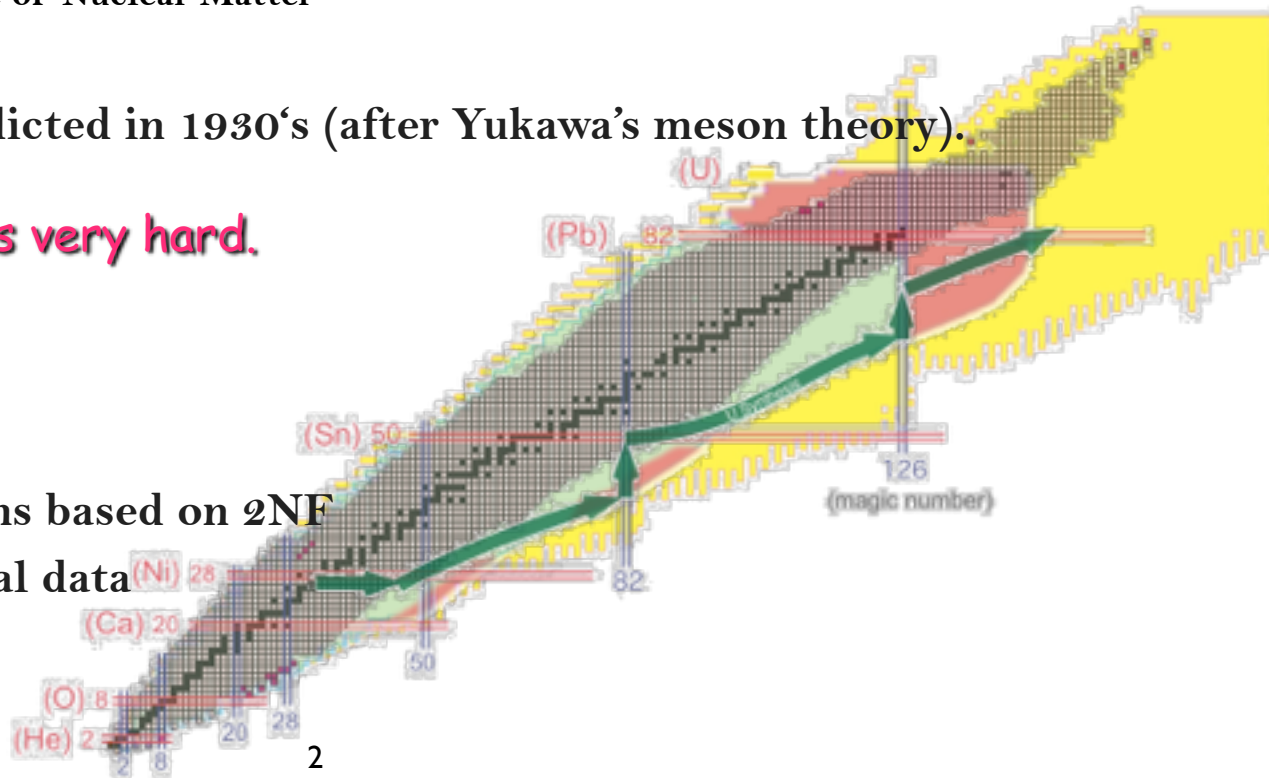
'90~

- Nucleon-Deuteron Elastic Scattering at Intermediate Energies
 - Binding Energies / Levels of Light Mass Nuclei
 - Equation of State of Nuclear Matter
- etc ...

Existence of 3NF was predicted in 1930's (after Yukawa's meson theory).

To find Evidence of 3NF is very hard.

- $3\text{NF} < 2\text{NF}$
- One needs,
 1. Reliable 2NF
 2. *Ab initio* calculations based on 2NF
 3. Precise experimental data

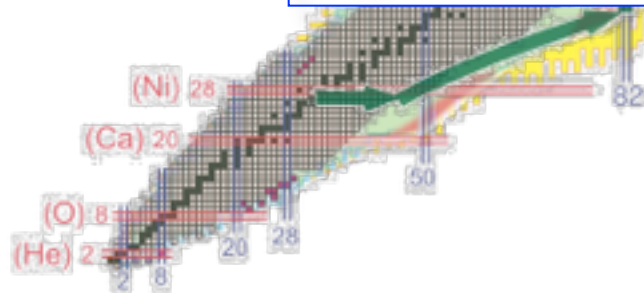
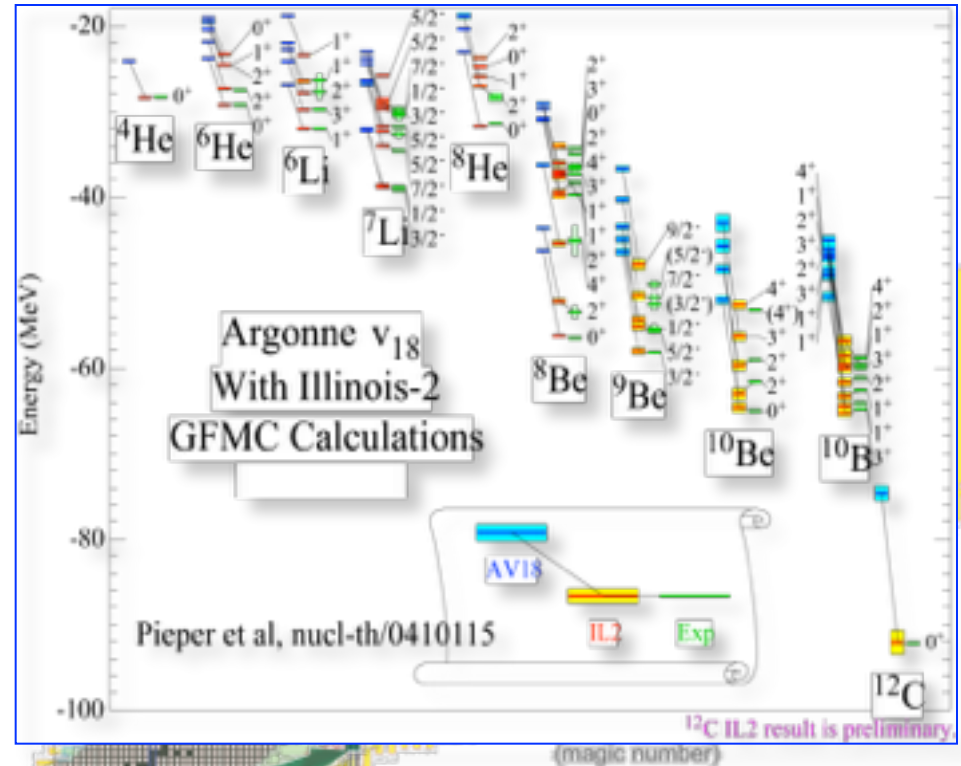


Where can we find 3NF effects ? - I -

3NFs in Finite Nuclei

Ab Initio Calculations for Light Nuclei

- Green's Function Monte Carlo
- No-Core Shell Model etc..



Where can we find 3NF effects ? - I -

3NFs in Finite Nuclei

Ab Initio Calculations for Light Nuclei

- **Green's Function Monte Carlo**
- **No-Core Shell Model** etc..

- 2NF provide less binding energies
- 3NF : well reproduce the data

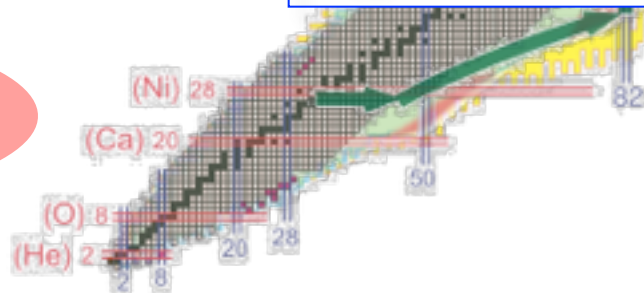
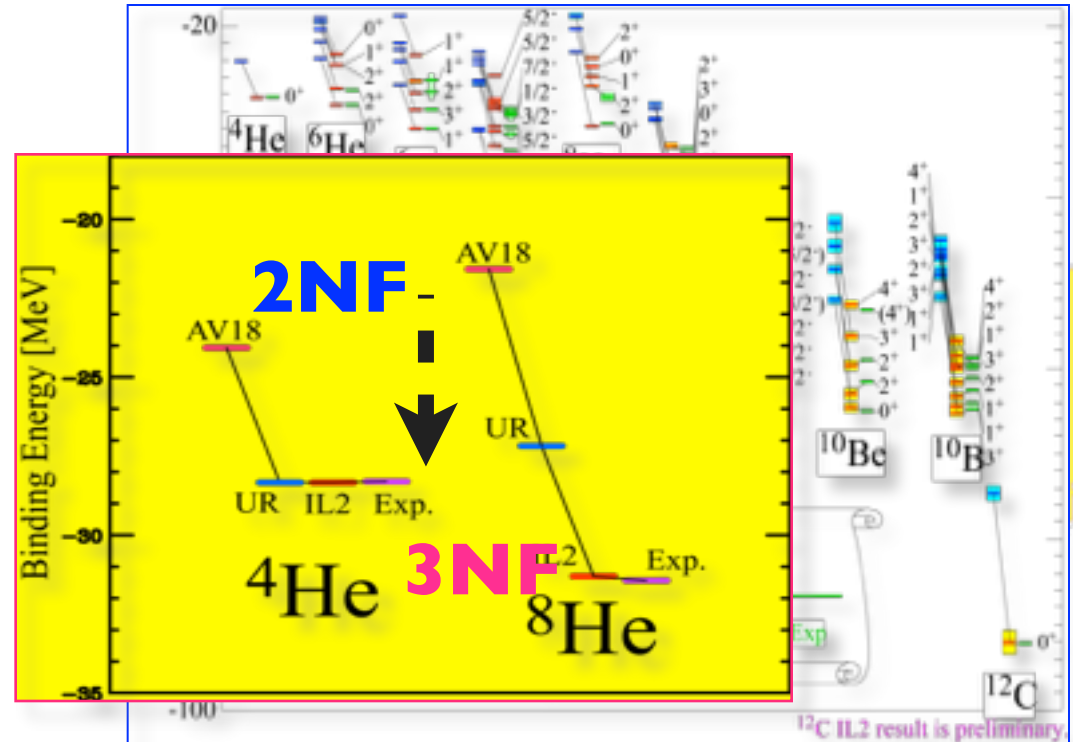
IL2 3NF (Illinois-II 3NF) :
2 π -exchange 3NF
+ 3 π -ring with Δ -isobar

3NF effects in B.E.

- 10-25%
- Attractive

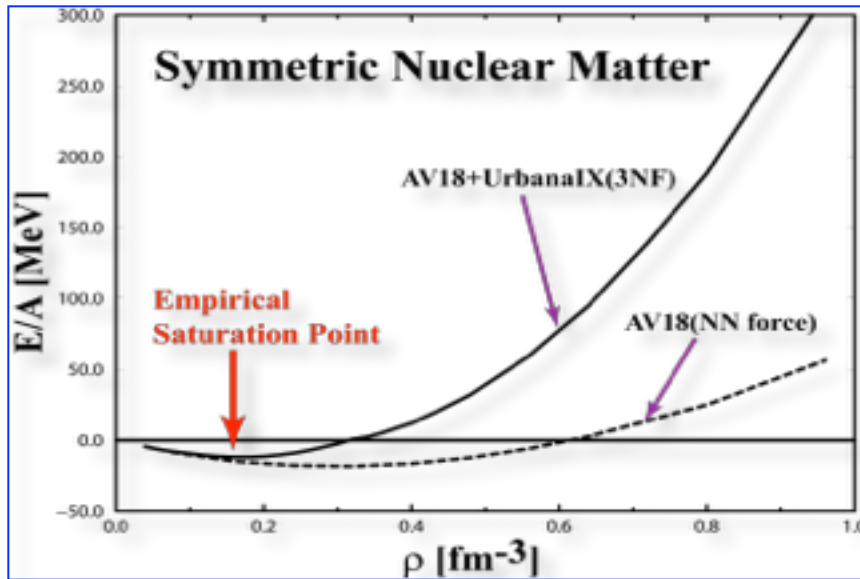
Note :

T=3/2 3NFs play important roles to explain B.E. in neutron rich nuclei.



Where can we find 3NF effects ? - II -

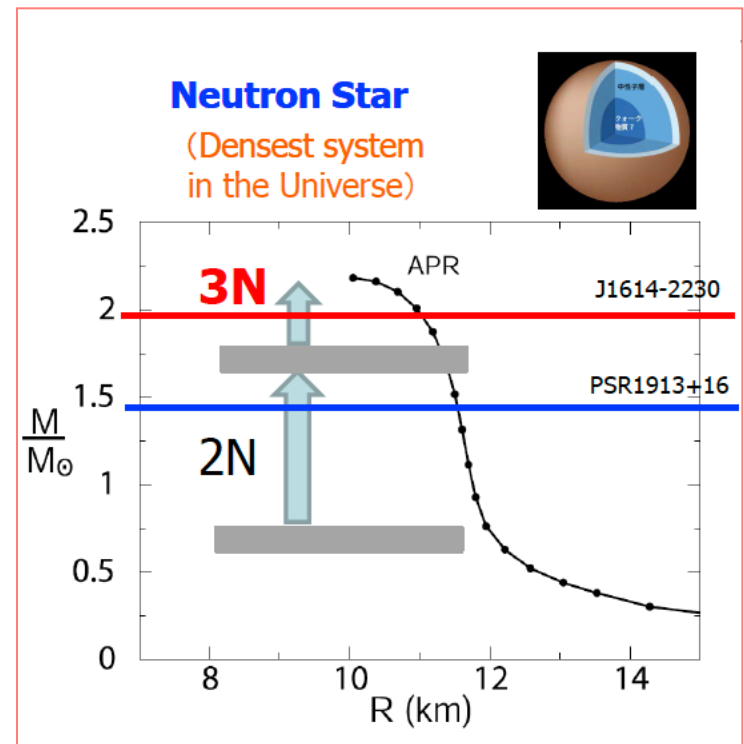
3NFs in Infinite Nuclei



A. Akmal et al., PRC 58, 1804('98)

- All NN potentials (AV18, Nijmegen I,II, CD Bonn) provide larger saturation point of Nuclear Matter.
- 3NF
 - shift to the empirical saturation point
 - significant at higher density

3NFs play important roles at high density



- Short range repulsive terms of 3NFs (3-Baryon Fs) are taken as key elements to understand 2 M(sun) neutron star.

- Understanding of 3NF is one key element to describe nuclear phenomena.
- How to constrain the properties of 3NF ?

Few-Nucleon Scattering is a good probe to study the dynamical aspects of 3NFs.

- ✓ Momentum dependence
- ✓ Spin dependence
- ✓ Iso-spin dependence

Few-Nucleon Scattering

a good probe to study the dynamical aspects of 3NFs.

- ✓ Momentum dependence
- ✓ Spin & Iso-spin dependence

Direct Comparison between Theory and Experiment

• Theory : Faddeev / Faddeev-Yakubovsky Calculations

Rigorous Numerical Calculations of 3, 4N System

2NF Input

- CDBonn
- Argonne V18 (AV18)
- Nijmegen I, II, 93

3NF Input

- Tucson-Melbourne
- Urbana IX
- etc..

2NF & 3NF Input

- Chiral Effective Field Theory

• Experiment : Precise Data

- $d\sigma/d\Omega$, Spin Observables (A_p , K_{ij} , C_{ij})

Extract fundamental information of Nuclear Forces.

Where is the hot spot for study of 3NFs ?

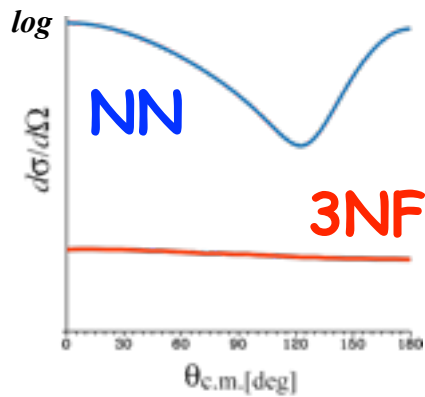
Nucleon-Deuteron Scattering

To study momentum & spin dependences
Iso-spin dependence : T=1/2 only

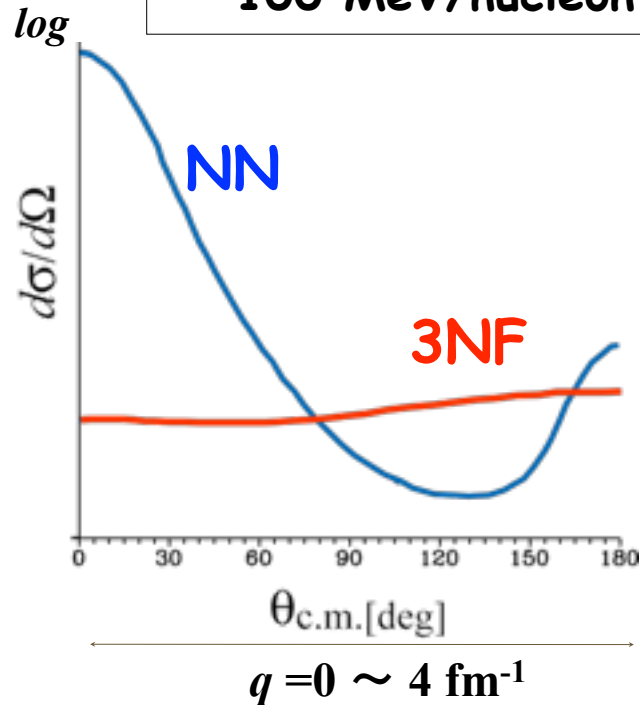
Predictions by H. Witala et al. (1998)

Cross Section minimum for Nd Scattering at ~ 100 MeV/nucleon

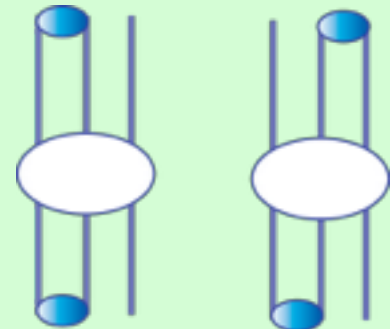
~ 10 MeV/nucleon



~ 100 MeV/nucleon

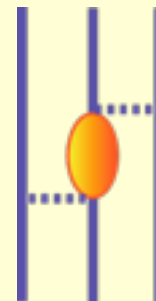


Nd scattering

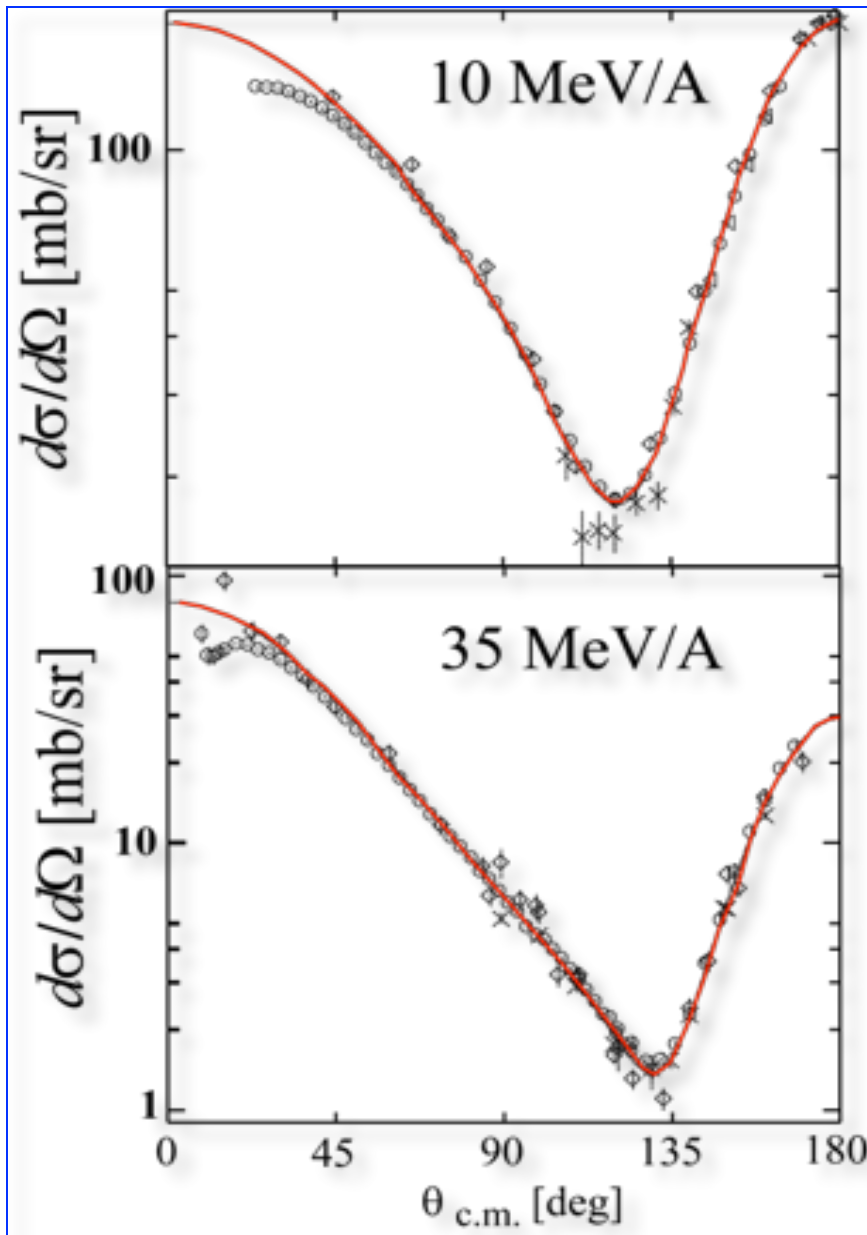


Forward Backward

3NF



Nd Scattering at Low Energies ($E \leq 30 \text{ MeV/A}$)



ⓐ High precision data are explained by Faddeev calculations based on 2NF.

No signatures of 3NF.

Exp. Data from
Kyushu, TUNL, Cologne etc..

W. Glöckle et al., Phys. Rep. 274, 107 (1996).

Summary of Precise Measurement of Nd Elastic Scattering at RIKEN/RCNP

$d + p$

RIKEN

1. **Differential Cross Section** at 70, 135 MeV/nucleon
2. **All Deuteron Analyzing Powers** (iT_{11} , T_{20} , T_{21} , T_{22})
at 70, 100, 135, 190, 250, 300 MeV/nucleon
3. **Deuteron to Proton Polarization Transfer Coefficients** at 135 MeV/nucleon

*N. Nakamoto et al., Phys. Lett. B 367, 60 (1996), H. Sakai et al., Phys. Rev. Lett. 84, 5288 (2000),
K. S. et al., Phys. Rev. C 65, 034003 (2002), K. S. et al., Phys. Rev. C 70, 014001 (2004),
K. S. et al., Phys. Rev. C 89, 064007 (2014) etc...*

$p + d$

RCNP

1. **Differential Cross Section** at 135, 250 MeV
2. **Proton Analyzing Powers** at 250 MeV
3. **Proton to Proton Polarization Transfer Coefficients** at 250 MeV

*K. Hatanaka et al., Phys. Rev. C. 66, 044002 (2002)
K. S. et al., Phys. Rev. Lett. 95, 162301 (2005)*

$n + d$

RCNP

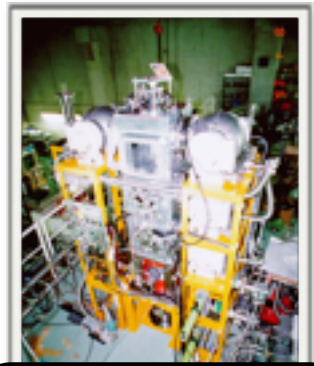
1. **Differential Cross Section** at 250 MeV
2. **Neutron Analyzing Powers** at 250 MeV

Y. Maeda et al., Phys. Rev. C 76, 014004 (2007)

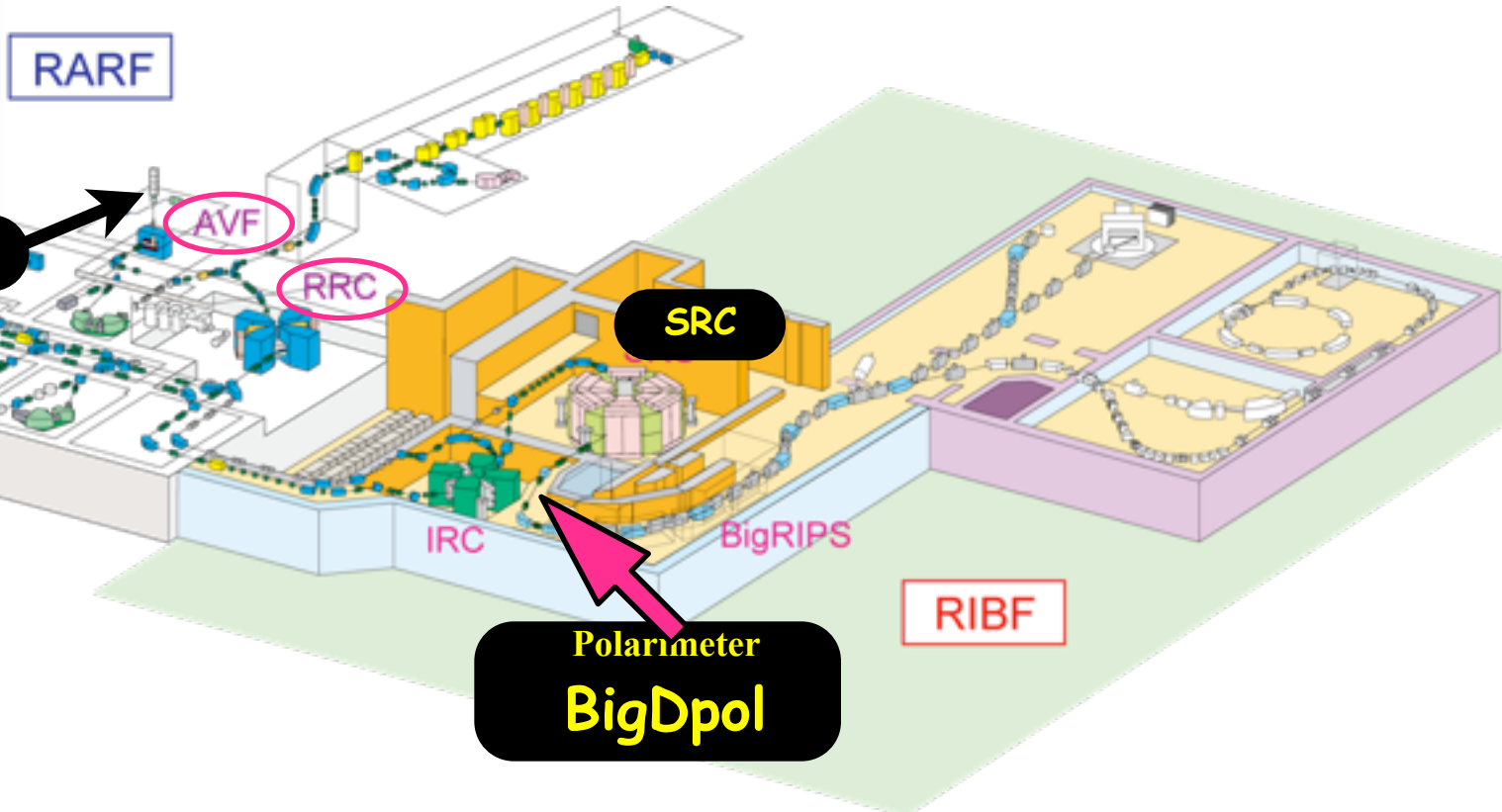
RIKEN RI Beam Factory (RIBF)

- Polarized d beam
 - acceleration by AVF+RRC : 65-135 MeV/nucleon
 - acceleration by AVF+RRC+SRC : 190-300 MeV/nucleon
 - polarization : 60-80% of theoretical maximum values
- Beam Intensity : < 100 nA

Spin axis of polarized d beams is freely controlled !



Polarized Ion Source



RARF

AVF

RRC

SRC

IRC

BigRIPS

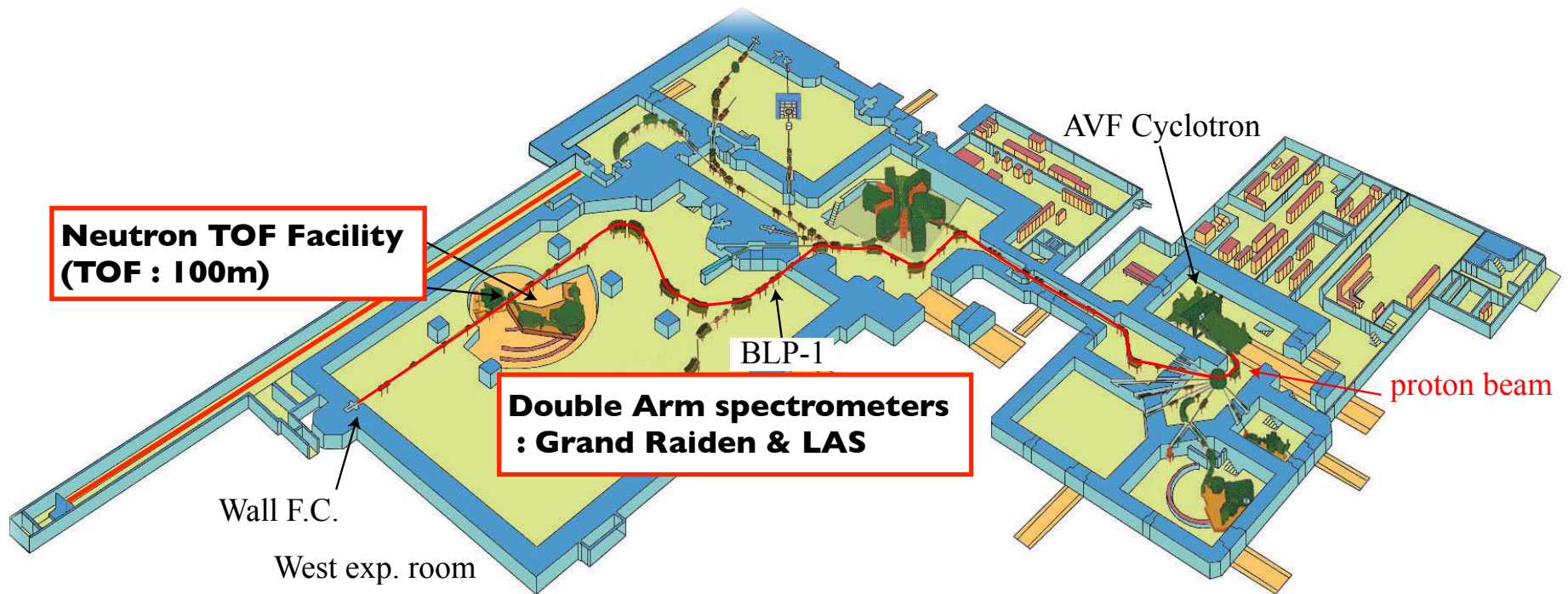
RIBF

SMART
(- 2005)

Polarimeter
BigDpol

RCNP, Osaka University

- Polarized p beam : 10 - 420 MeV/nucleon
- Polarized d beam : 5 - 100 MeV/nucleon
 - Polarizations : < 70 %
- (pol.) Neutron beams by ${}^7\text{Li}(p,n)$
- Beam Intensity : < $1\mu\text{A}$



Nd Elastic Scattering Data at Intermediate Energies

pd and *nd* Elastic Scattering at 65–400 MeV/nucleon

Observable	100	200	300	400
$\frac{d\sigma}{d\Omega}$	•••••••••• •	•••••••••• •••	•••••••••• •	•
$\vec{p} \rightarrow \vec{n}$ A_y^p A_y^n		•••••••••• •	•••••••••• •	•
\vec{d} iT_{11} T_{20} T_{22} T_{21}	•••••••••• •••••••••• •••••••••• ••••••••••	•••••••••• •••••••••• •••••••••• ••••••••••	•••••••••• •••••••••• •••••••••• ••••••••••	•
$\vec{p} \rightarrow \vec{p}$ $K_y^{y'}$ $K_x^{x'}$ $K_x^{z'}$ $K_z^{x'}$ $K_z^{z'}$			•••••••••• •••••••••• •••••••••• •••••••••• ••••••••••	
$\vec{d} \rightarrow \vec{p}$ $K_y^{y'}$ $K_{xx}^{y'}$ $K_{yy}^{y'}$ $K_{xz}^{y'}$	•••••••••• •••••••••• •••••••••• ••••••••••	•••••••••• •••••••••• •••••••••• ••••••••••		
$\vec{p} \rightarrow \vec{d}$ $K_y^{y'}$				•
$\vec{p} \vec{d}$ $C_{i,j}$ $C_{i,j,k}$		•••••••••• ••••••••••	•••••••••• ••••••••••	

~2018

- High precision data of $d\sigma/d\Omega$ & Spin Observables from RIKEN, RCNP, KVI, IUCF
- Energy dependent data
 - ✓ $d\sigma/d\Omega$
 - ✓ Proton Analyzing Power
 - ✓ Deuteron Analyzing Powers

dp elastic scattering

Cross Section

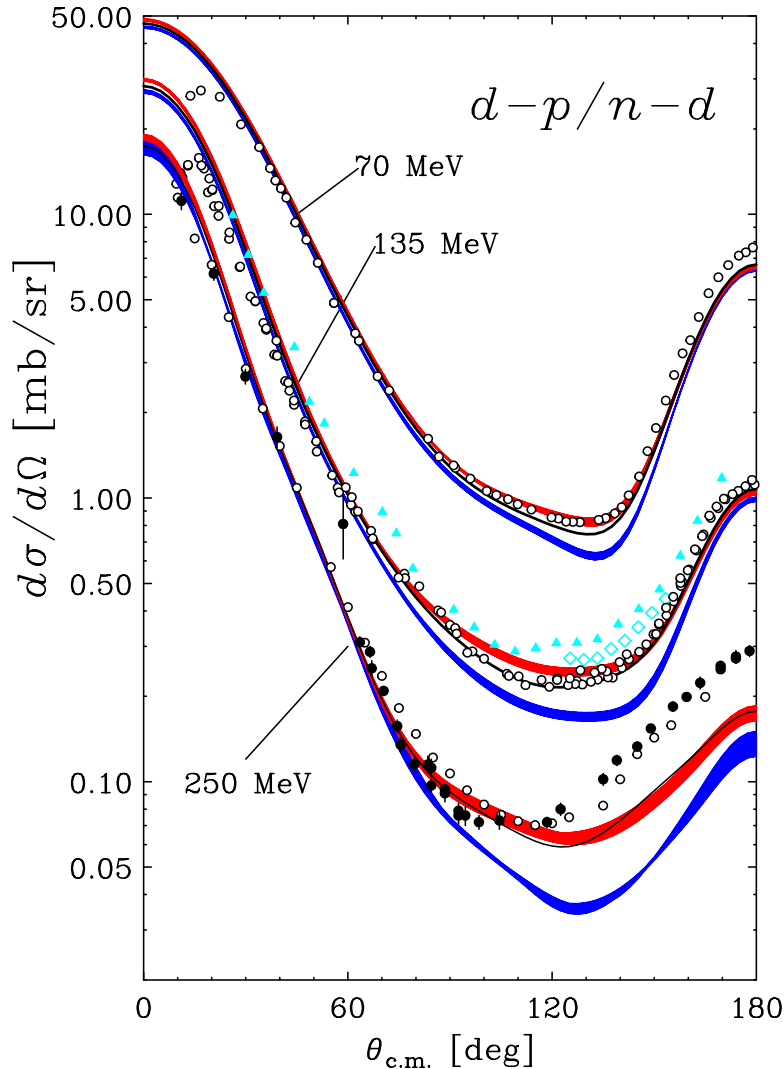
K.S. et al., Phys. Rev. C. 65,034003 (2002)

K.Hatanaka et al., Phys. Rev. C 66,044002 (2002)

K.S. et al., Phys. Rev. Lett. 95,162301 (2005)

Y. Maeda et al., Phys. Rev. C 76,014004 (2007)

Differential Cross Section at 70 - 250 MeV/nucleon



● NN only

⊗ Large discrepancy

in the backward region

● 3NF :

⊗ improve the agreement

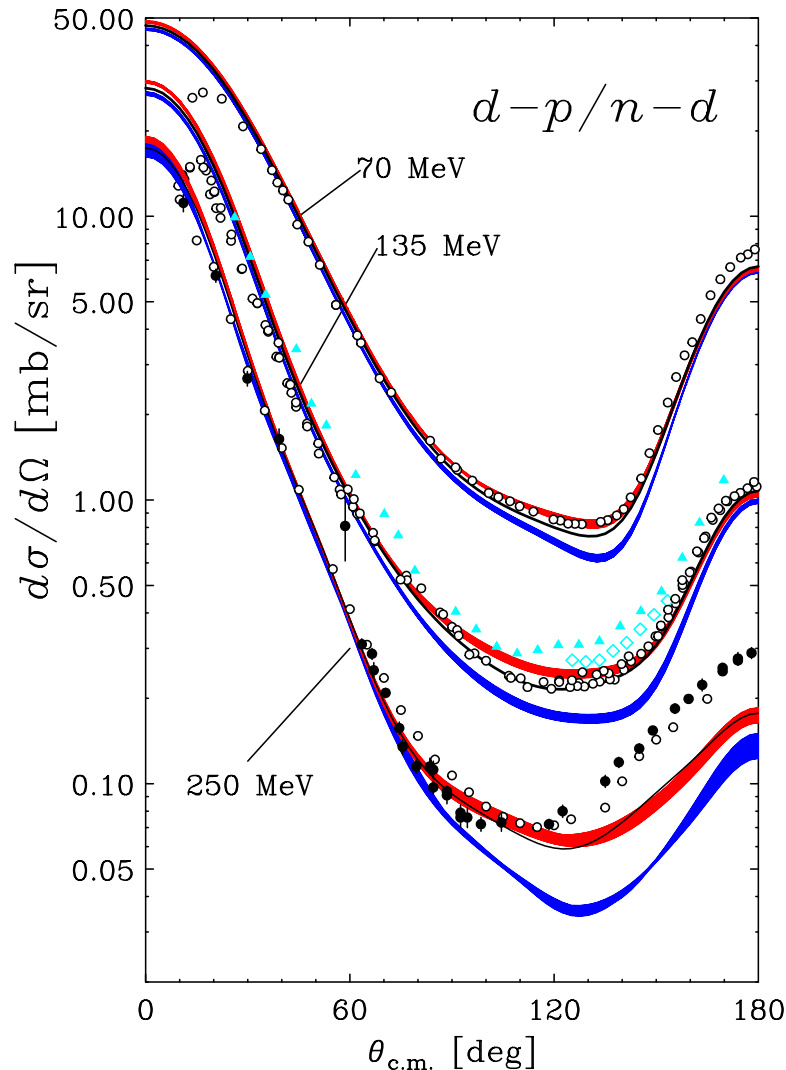
⊗ not enough at very backward angles at higher energies

■ NN (CDBonn, AV18, Nijm I,II)

■ TM'(99) 3NF +
NN(CD Bonn, AV18, Nijm I,II)

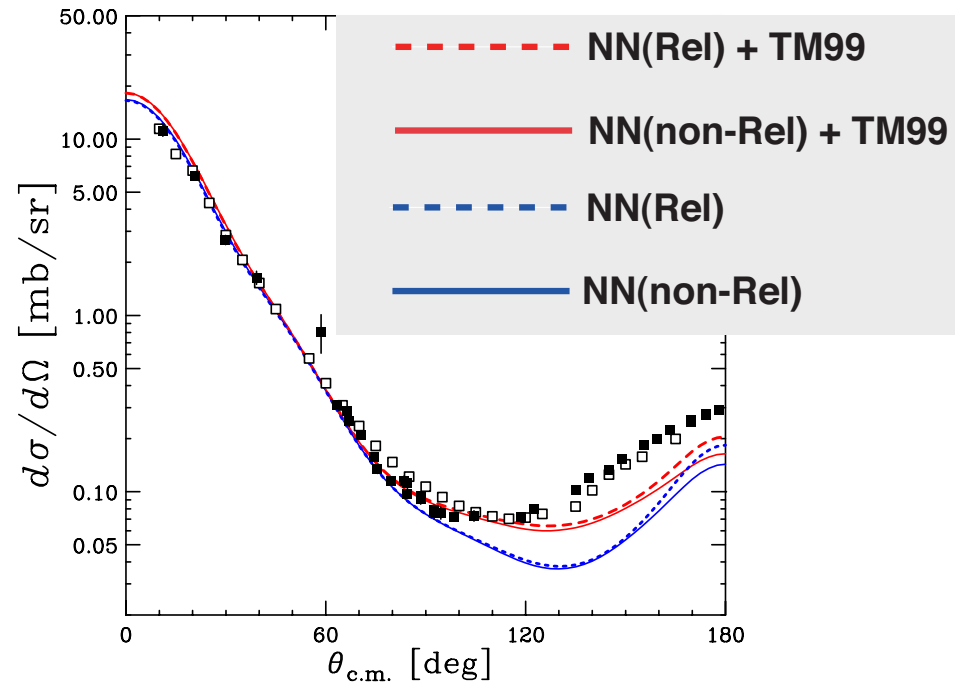
— Urbana IX 3NF+AV18

Differential Cross Section at 70 - 250 MeV/nucleon



Relativistic Faddeev
Calculations with TM'99 3NF

pd/nd @ 250 MeV



Relativistic effects are visible
at backward angles, but small.

Backward angles :
Shorter range 3NFs ?
Other dynamics ?

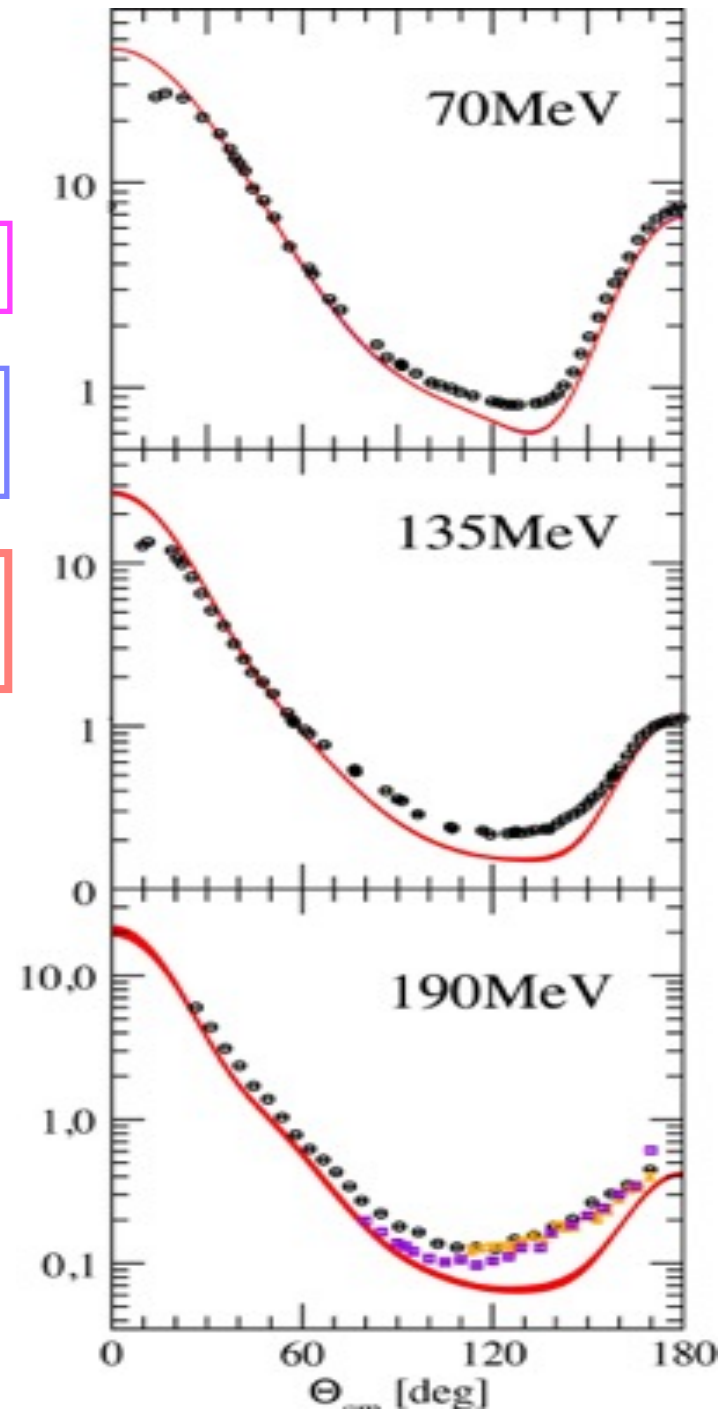
Differential Cross Section at 70 - 190 MeV/nucleon

Chiral EFT NN potential (N4LO)

● NN only

Large discrepancy in the backward region

● It is very interesting to see how χ EFT
3NFs describe the cross section !

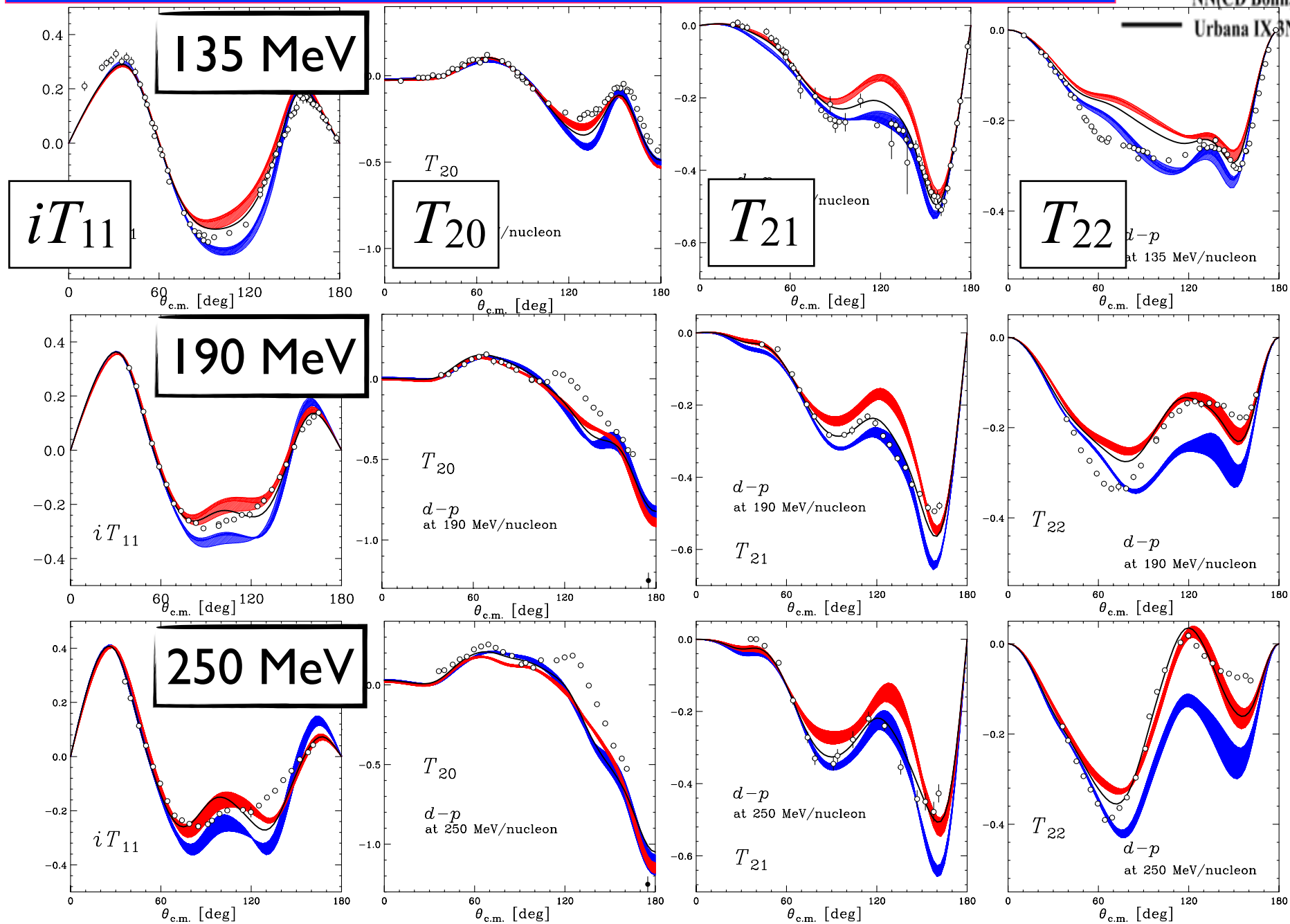


dp elastic scattering

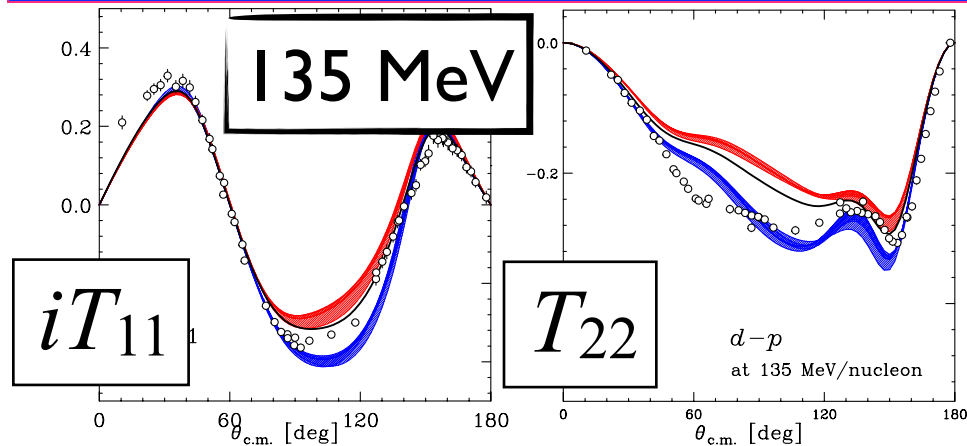
Spin Observables
(Analyzing Powers)

Deuteron Analyzing Powers at 135, 190, 250 MeV/nucleon

■ NN (CDBonn, AV18)
■ TM'(99) 3NF +
 NN(CD Bonn, AV18)
— Urbana IX 3NF+A

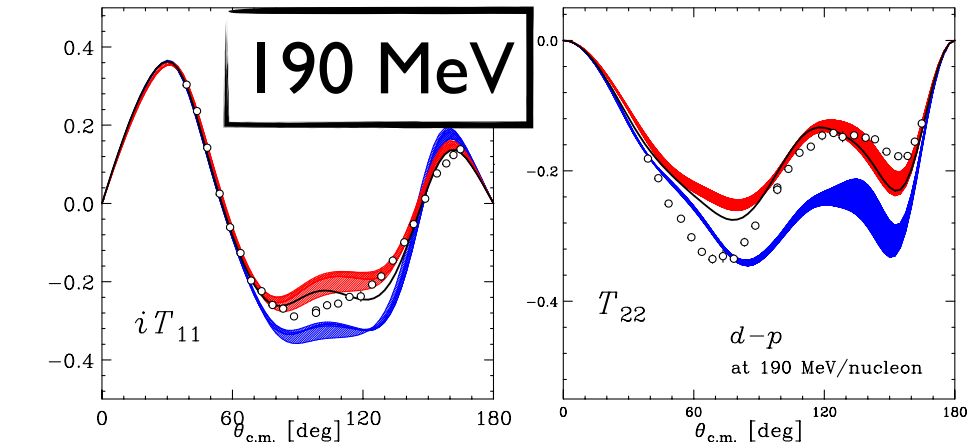


Deuteron Analyzing Powers at 135, 190, 250 MeV/nucleon



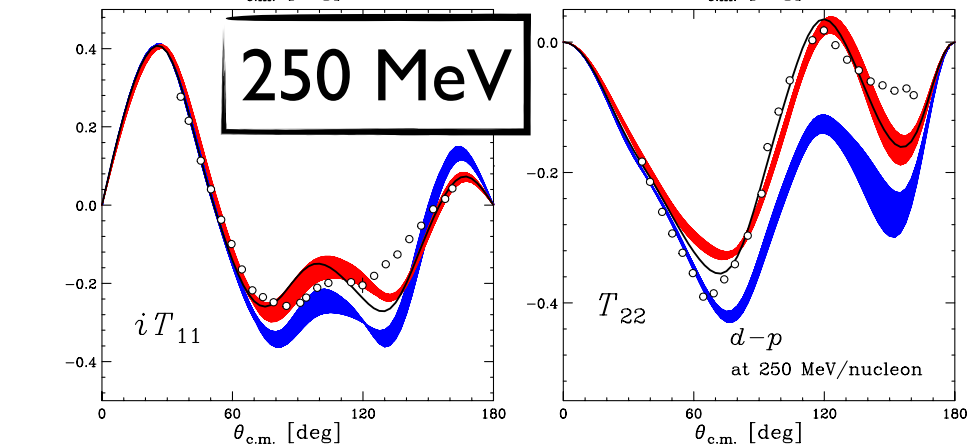
● NN only

- Large discrepancy in the backward angles



● + 2π 3NF at 135 MeV

- results are NOT always similar to the cross section.



● + 2π 3NF at 190, 250 MeV

- improve the agreement

- not enough at very backward angles

- NN (CDBonn, AV18, Nijm I,II)
- TM'(99) 3NF + NN(CD Bonn, AV18, Nijm I,II)
- Urbana IX 3NF+AV18

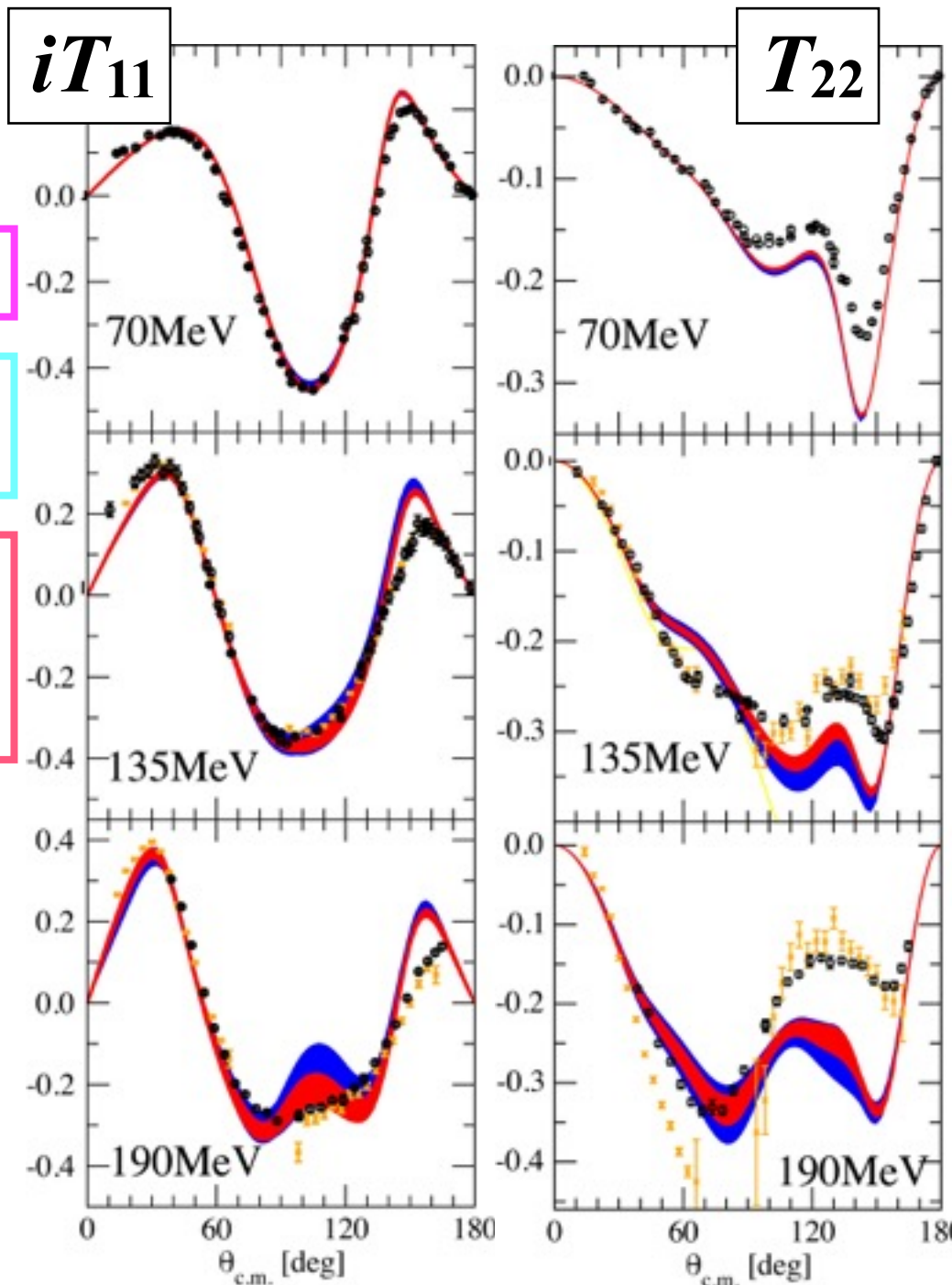
Analyzing Powers at 70 - 190 MeV/nucleon

Chiral EFT N3LO & N4LO NN pot.

Vector analyzing power (iT_{11}):
Good agreements to NN forces

Large discrepancies
in Tensor analyzing powers (T_{22})

➔ Rooms for 3NFs



Results of Comparison - dp elastic scattering -

- Cross Section :
 - **3NFs are clearly needed.**
- Spin Observables :
 - Not always described by adding 3NFs
 - **3NF effects are spin dependent.**
- **Serious discrepancy** at backward angles at higher energies
 - : Short-range terms of 3NFs ?
- It is interesting to see how $\chi^{\text{EFT}}_{\text{NN+NNN}}$ potentials explain the exp. data.

$p + {}^3\text{He}$ scattering
- Next Step -

$p+{}^3\text{He}$ scattering

4-nucleon scattering

First Step from Few to Many

Approach to iso-spin dependence of 3NFs
 $T=3/2$ 3NFs

Large 3NF effects

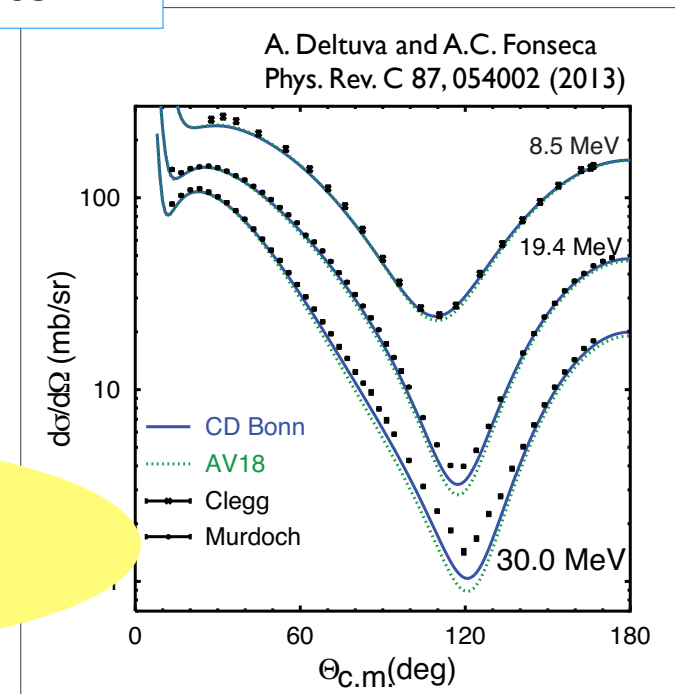
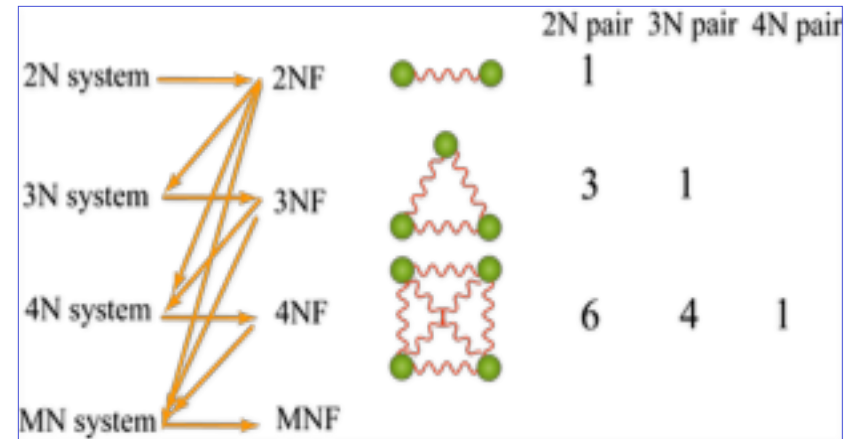
in cross section minimum at intermediate energies

4NF effects

Theory in Progress

Calculations above 4-body breakup threshold energy
 open new possibilities of 3NF study in 4N scat.

Discrepancies in dcs minimum at higher energies
New rooms for 3NF study



New ^3He Analyzing Power exp./data

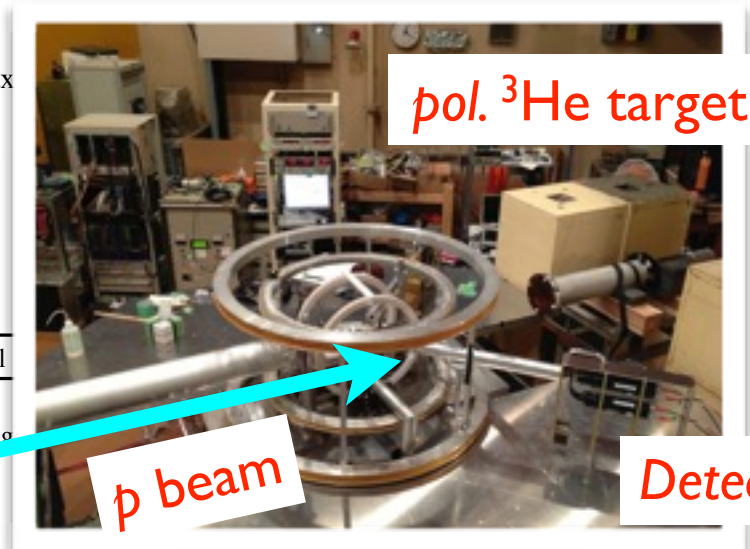
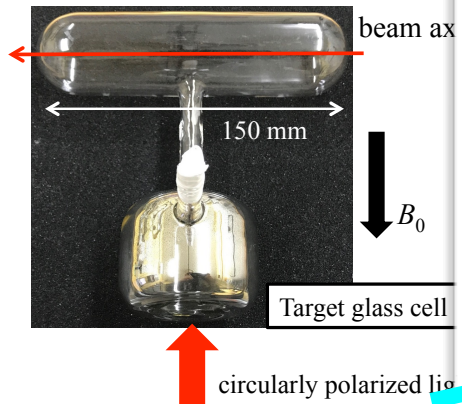
$p + ^3\text{He}$ at 70 MeV

from CYRIC, Tohoku Univ.

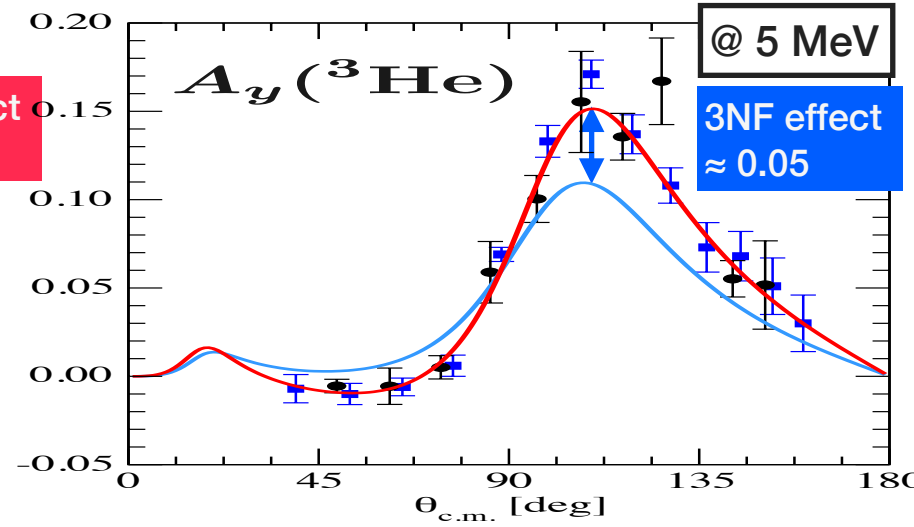
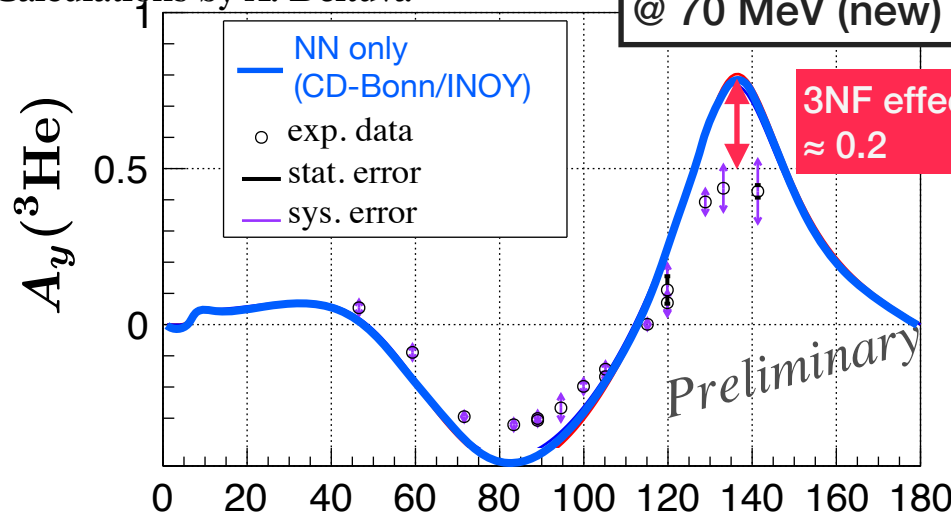
New pol- ^3He target

- 3 atm ($\approx 2 \text{ mg/cm}^2$)
- $\approx 50\%$ polarization

Thanks !
 GE180 glass (Target cell)
 was provided by
 Prof. Wooyoung Kim,
 Kyungpook National University, Korea.



Calculations by A. Deltuva

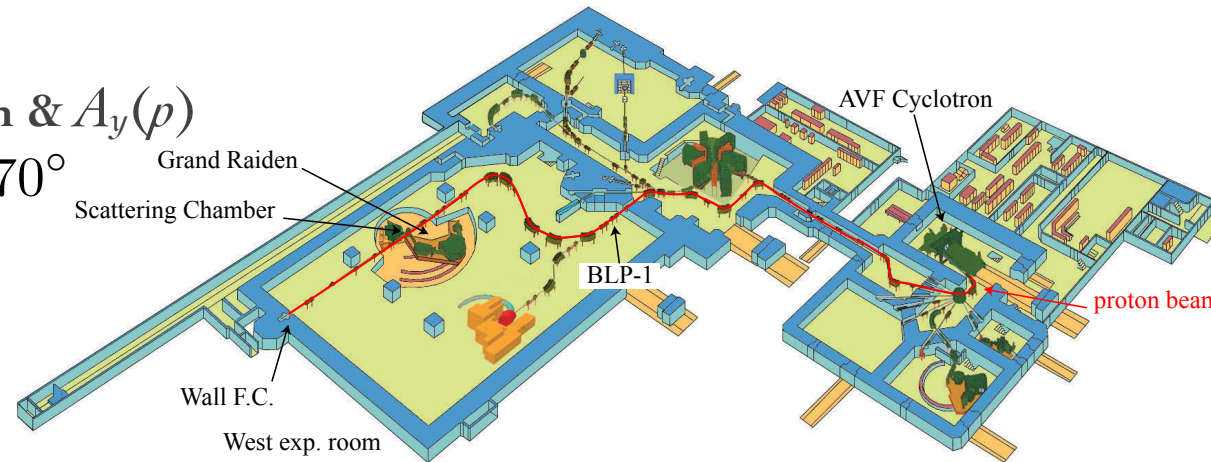


Large 3NF effects are indicated at 70 MeV.

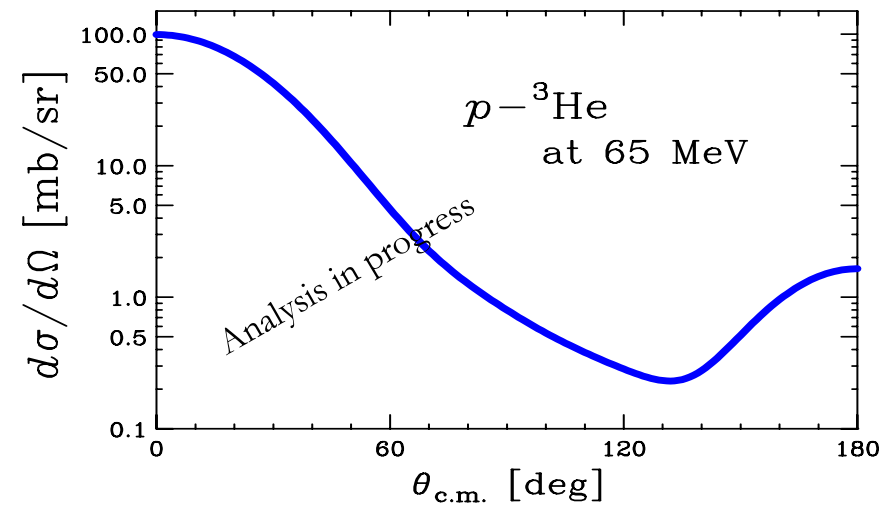
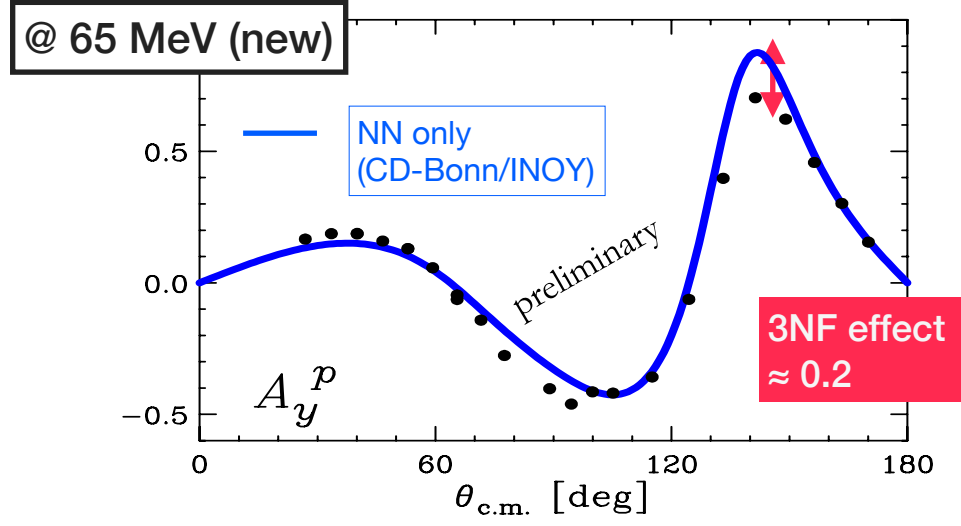
New Proton Analyzing Power exp./data from RCNP, Osaka Univ.

$\vec{p} + {}^3\text{He}$ at 65 MeV

- ◆ Observables : Cross section & $A_y(p)$
- ◆ Angles : $\theta_{\text{c.m.}} = 27^\circ - 170^\circ$



Calculations by A. Deluva

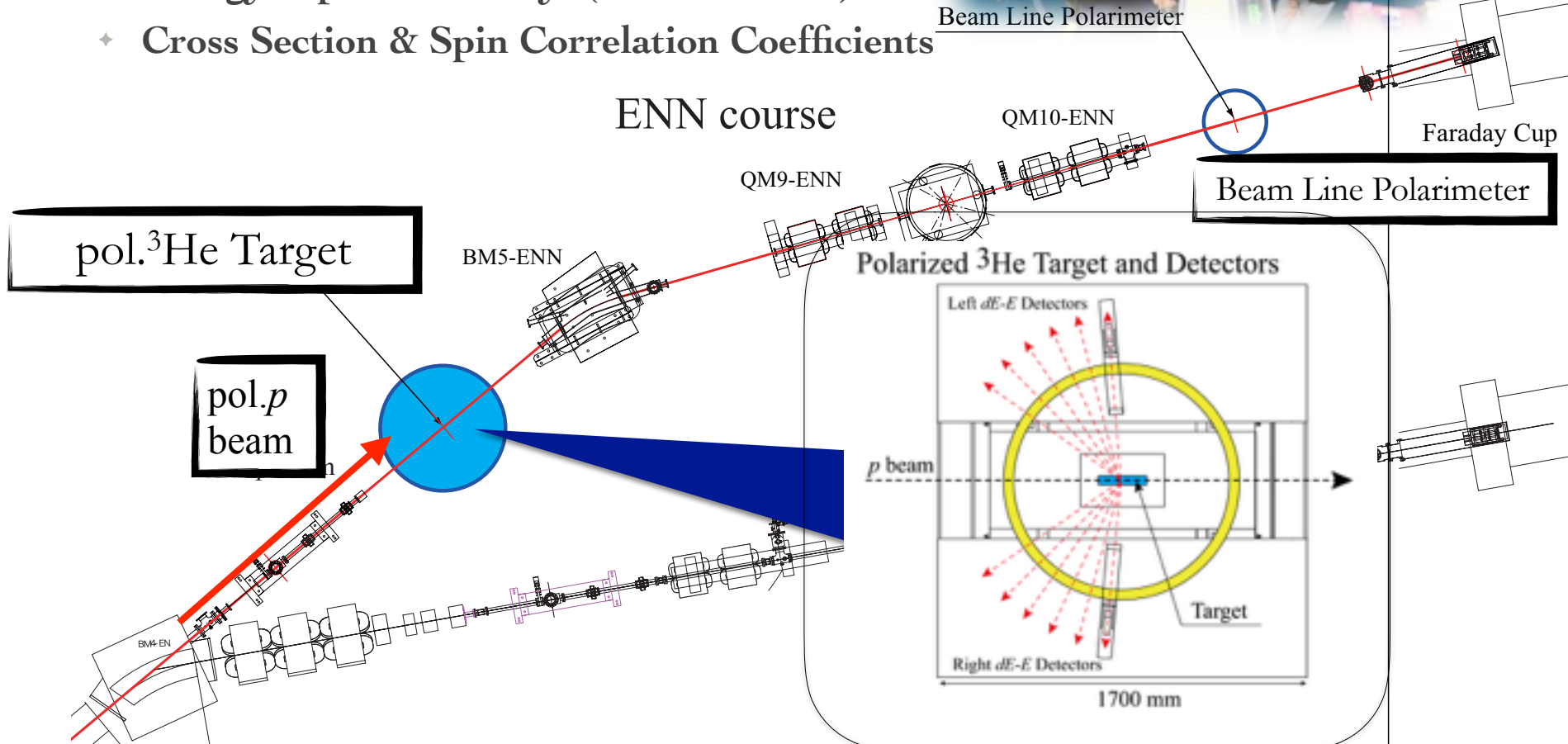


3NF effects can be seen in the cross section minimum.

New Experiment : pol.p+pol. ^3He at RCNP

in preparation

- ◆ First experiment : p+ ^3He at 135 MeV
 - ◆ Observables : $A_y(p)$, $A_y(^3\text{He})$ & $C_{y,y}$
 - ◆ Angles : $\theta_{\text{c.m.}} = 47^\circ - 156^\circ$
- ◆ Future Planning
 - ◆ Energy dependent study (65 - 200MeV)
 - ◆ Cross Section & Spin Correlation Coefficients



Summary (1/2)

Few-Nucleon Scattering

is a good probe to investigate the dynamics of 3NFs .

- Momentum, Spin & Iso-spin dependence - .

Nucleon-Deuteron Elastic Scattering

Precise data of $d\sigma/d\Omega$ and spin observables at 70- 300 MeV/nucleon from RIKEN/RCNP

Cross Sections : Large discrepancy at backward angles. 3NFs are clearly needed.

Spin Observables : 3NF effects are spin dependent.

Serious discrepancy at backward angles at higher energies : short-range terms of 3NFs ?

It is interesting to see how ChEFT NN+NNN potentials explain the data.

$p+^3\text{He}$ scattering

- Approach to Iso-spin states of $T=3/2$ 3NF
- Faddeev-Yakubovsky calculations : New possibilities for 3NF study in 4N Scatt.

New Data from CYRIC & RCNP : ^3He & p Analyzing powers, & Spin Correlation Coefficient

Summary (2/2)

Future Plan

Nucleon-Deuteron Scattering :

Extend to Measurement of Spin Correlation Coefficients

p+³He Scattering : Energy dependent study

& Other reaction channels : e.g. ³He(p,n)

Study of 3NF effects in Nuclear Reaction

Study of T=3/2 three-nucleon systems (3p, 3n-states)

RIBF-d Collaboration

Tohoku University

K. Sekiguchi, K. Miki, Y. Wada, A. Watanabe, D. Eto, T. Akieda, H. Kon,
J. Miyazaki, T. Taguchi, U. Gebauer, K. Takahashi, T. Mashiko

RIKEN Nishina Center

N. Sakamoto, H. Sakai, T. Uesaka, M. Sasano, Y. Shimizu

Kyushu University

T. Wakasa, S. Sakaguchi, J. Yasuda, A. Ohkura, S. Shindo, U. Tabata

Miyazaki University

Y. Maeda, T. Saito, S. Kawakami, T. Yamamoto

CNS, University of Tokyo

K. Yako, M. Dozono, R. Tang, S. Kawase, Y. Kubota, C.S. Lee

RCNP, Osaka University

H. Okamura

Kyungpook National University

S. Chebotaryov, E. Milman



$p+{}^3\text{He}$ Collaboration

Department of Physics, Tohoku University

K. Sekiguchi, Y. Wada, Y. Shiokawa, A. Watanabe, S. Nakai, K. Miki,
T. Mukai, S. Shibuya, M. Watanabe, K. Kawahara, D. Sakai,
T. Taguchi, D. Eto, T. Akieda, H. Kon, M. Inoue, Y. Utsuki

CYRIC, Tohoku University

M. Itoh

KEK

T. Ino

RCNP, Osaka University

K. Hatanaka, A. Tamii, H.J. Ong, N. Kobayashi

Kyushu University

T. Wakasa

Miyazaki University

Y. Maeda

RIKEN Nishina Center

H. Sakai, T. Uesaka

NIRS

T. Wakui



$p+{}^3\text{He}$ scattering

at 5.54 MeV

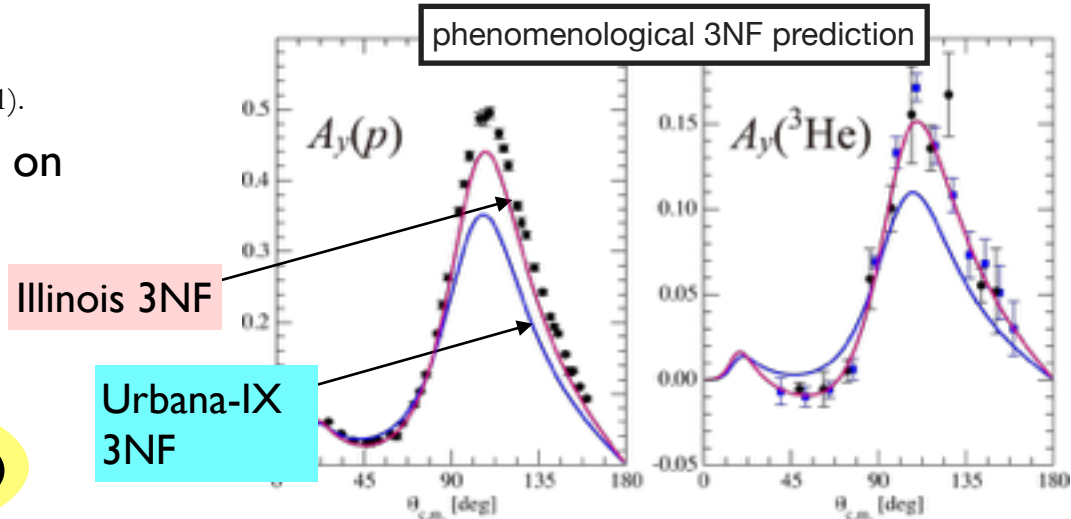
Theory in Progress

Viviani et al., Phys. Rev. Lett. 111, 172302(2011).

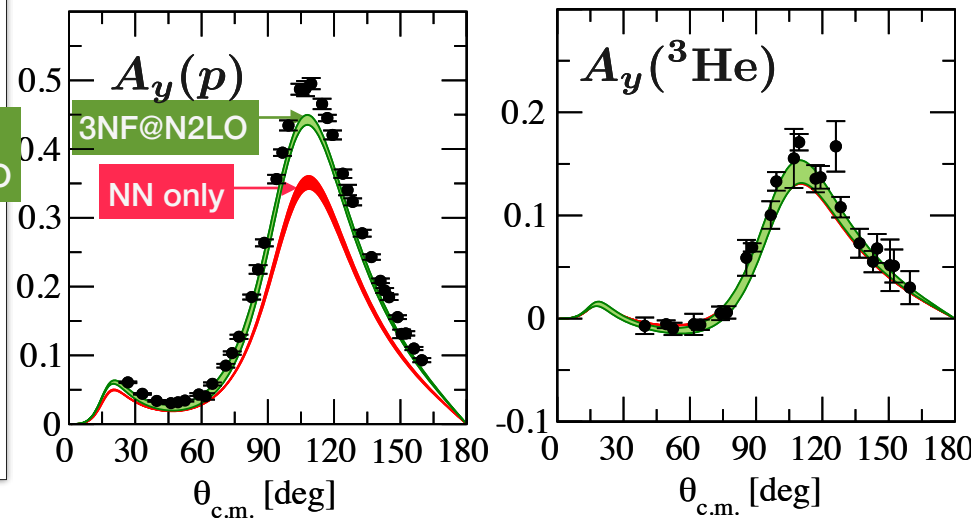
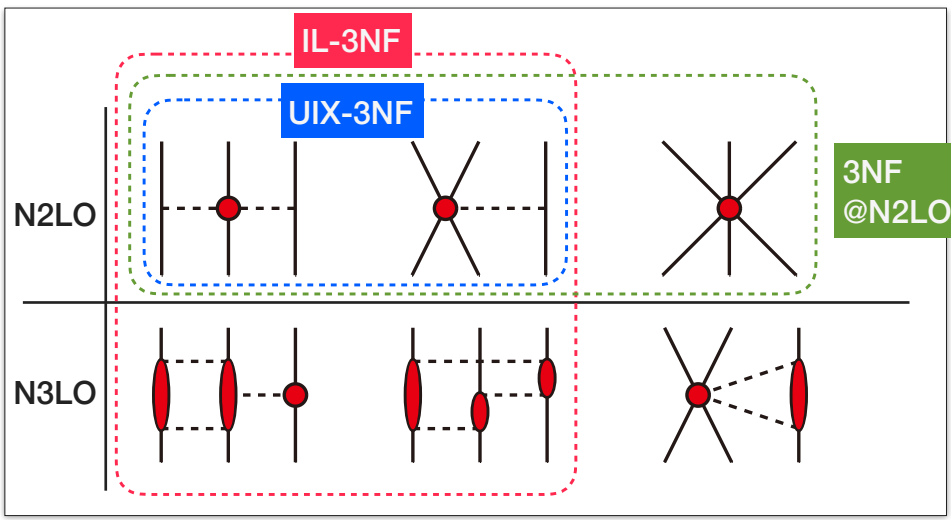
Pisa Gr. succeeds in calculations based on

- AV18 + Illinois 3NF
- χEFT (3NF : N2LO)

3 π -ring with Δ 3NFs are significant for $A_y(p)$ & $A_y({}^3\text{He})$ (Iso-spin dependence).



chiral EFT prediction up to N²LO



Now, it is interesting to study at higher energies for pol. observables with high accuracy!